

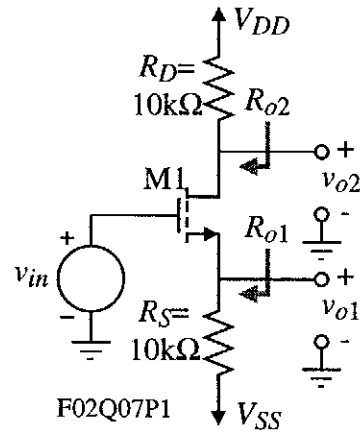
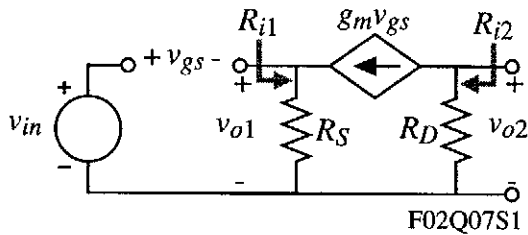
QUIZ NO. 7 - SOLUTION

(Average Score = 6.8/10 for only those students taking the quiz)

If $k_n = 1\text{mA/V}^2$, $V_{TN} = 1\text{V}$, $I_{DS} = 0.5\text{mA}$ and $\lambda = 0\text{V}^{-1}$, find the numerical values of the following small signal functions: v_{o2}/v_{in} , v_{o1}/v_{in} , R_{o1} and R_{o2} .

Solution

Small signal model:



$$g_m = \sqrt{2 \cdot k_n \cdot I_{DS}} = \sqrt{2 \cdot 1 \cdot 0.5} = 1\text{mS}$$

$$\frac{v_{o2}}{v_{in}} = \left(\frac{v_{o2}}{v_{gs}} \right) \left(\frac{v_{gs}}{v_{in}} \right) = (-g_m R_D) \left(\frac{1}{1+g_m R_S} \right) = \left(\frac{-g_m R_D}{1+g_m R_S} \right) = \frac{-10}{11} = \underline{-0.909 \text{ V/V}}$$

$$\frac{v_{o1}}{v_{in}} = \left(\frac{v_{o1}}{v_{gs}} \right) \left(\frac{v_{gs}}{v_{in}} \right) = (g_m R_S) \left(\frac{1}{1+g_m R_S} \right) = \left(\frac{g_m R_S}{1+g_m R_S} \right) = \frac{10}{11} = \underline{+0.909 \text{ V/V}}$$

(This circuit happens to be a phase splitter because it creates a \pm version of the input multiplied times 0.909 in this case.)

$$R_{o2} = R_D = \underline{10\text{k}\Omega}$$

R_{o1} probably requires the use of a small signal model to make sure to avoid mistakes.

We see that,

$$i_t = \frac{v_s}{R_S} + g_m v_s = v_s \left(\frac{1}{R_S} + g_m \right) = v_t \left(\frac{1}{R_S} + g_m \right)$$

$$\therefore R_{o1} = \frac{v_t}{i_t} = \left(\frac{R_S}{1+g_m R_S} \right) = \frac{10\text{k}\Omega}{11} = \underline{0.909\text{k}\Omega}$$

