# Homework Assignment No. 1 – Solutions

#### Problem 1

(a.) The first thing to do is to find Thevenin's equivalent circuit seen from the diode.

The Thevenin voltage is,

$$V_{TH} = V_{IN} \left(\frac{2}{3} - \frac{1}{3}\right) = \frac{V_{IN}}{3}$$

The Thevenin resistance is,

$$R_{TH} = 1k\Omega ||2k\Omega + 1k\Omega ||2k\Omega = \frac{4}{3} k\Omega$$

The equivalent circuit now becomes,

Now , with  $V_{IN} = 10$ V, we know the diode is forward biased. Therefore, replacing it with a short-circuit gives,

$$V_D = \underline{0V}$$
 and  $I_D = \frac{10}{3} x \frac{3}{4k\Omega} = \underline{2.5 \text{ mA}}$ 

(b.) With  $V_{IN}$  = -10V, we know the diode is reverse biased. Therefore replacing it with an open-circuit gives,

$$V_D = -3.33 \text{V}$$
 and  $I_D = 0 \text{ mA}$ 





#### Problem 2

If  $\beta_F = 100$  and  $V_{BEQ} = 0.6$ V, solve for the dc values of  $I_B$ ,  $I_C$ ,  $I_E$ ,  $V_B$ .  $V_C$ . and  $V_E$  of the transistor circuit shown.

## <u>Solution</u>

The first step is to find a Thevenin equivalent circuit seen from the base to ground. This circuit is shown below where

$$V_{BB} = \frac{10 \cdot R_1}{R_1 + R_2} = 5$$
 and  $R_B = R_1 || R_2 = 50$  k $\Omega$ 





The base current,  $I_B$ , can be found from the base-emitter voltage loop.

$$V_{BB} = I_B R_B + V_{BEQ} + I_B (1+\beta_F) R_E \rightarrow I_B = \frac{V_{BB} - 0.6}{R_B + (1+\beta_F) R_E} = \frac{4.4 \text{V}}{151 \text{k}\Omega} = \underline{29.14 \mu \text{A}}$$
  
$$\therefore \qquad I_C = \beta_F I_B = \underline{2.914 \text{m}} \text{ and } \quad I_E = I_C + I_B = \underline{2.943 \text{m}} \text{A}$$

The voltages of the transistor can be found as follows.

$$V_C = 10V - I_C R_C = 10 - 2.914 \text{mA} \cdot 2\text{k}\Omega = 10 - 5.83 = \underline{4.17V}$$
$$V_E = I_E R_E = 2.942 \text{mA} \cdot 1\text{k}\Omega = \underline{2.942V}$$
$$V_B = V_E + V_{BEO} = 2.942 + 0.6 = \underline{3.543V}$$

A pnp BJT circuit is shown. (a.) Find the dc values of  $I_E$ ,  $I_C$ ,  $I_B$ ,  $V_E$ ,  $V_C$  and  $V_B$  if  $\beta = 50$  and  $V_{EB}$ (on) = 0.65V. (b.) For what value of  $R_C$  does the BJT become saturated? (Recall that saturation of a BJT corresponds to the *BE* and *BC* junctions forward biased.) <u>Solution</u>

(a.) Note that 
$$I_E = 1\text{mA}$$
  $\alpha_F = \frac{\beta_F}{1 + \beta_F} = \frac{50}{51} = 0.98$   
 $\therefore I_C = \alpha_F I_E = 0.98 \cdot 1\text{mA} = 0.98\text{mA} \Rightarrow I_C = 0.98\text{mA}$   
 $I_B = \frac{I_C}{\beta_F} = \frac{0.98\text{mA}}{50} = 19.6\mu\text{A} \Rightarrow I_B = 19.6\mu\text{A}$   
Now,  $V_B = I_B \cdot 100\text{k}\Omega = 1.96\text{V} \Rightarrow V_B = 1.96\text{V}$   
 $V_E = V_B + V_{EB}(\text{on}) = 1.96\text{V} + 0.65\text{V} = 2.61\text{V} \Rightarrow V_E = 2.61\text{V}$   
Finally,  $V_C = -10\text{V} + I_C \cdot 10\text{k}\Omega = -10\text{V} + 0.98\text{mA} \cdot 10\text{k}\Omega = -0.2\text{V} \Rightarrow V_C = -0.2\text{V} \approx 0\text{V}$ 

(b.) Saturation occurs when  $V_{BC} = 0$  of  $V_B = V_C$ . Therefore,  $V_C = 1.96V$ . The current through  $R_C$  is still 0.98mA, so solving for  $R_C$  gives,

$$R_C = \frac{V_C + 10V}{I_C} = \frac{11.96V}{0.98\text{mA}} = 12.20\text{k}\Omega \implies \boxed{R_C = 12.2\text{k}\Omega}$$



1mA

 $\bullet V_E$ 

F=50

 $V_B$ 

+10V

## Problem 4

The NMOS transistor shown has the parameters of  $K_n = 1 \text{mA/V}^2$ ,  $V_{TN} = 1 \text{V}$  and  $\lambda_N = 0 \text{V}^{-1}$ . In saturation, the large signal model is  $i_D = 0.5 K_n (v_{GS} - V_T)^2$ .

a.) Assume the NMOS transistor is saturated and find the value of  $R_S$  that gives a drain current of 0.2mA.

b.) What value of  $R_D$  will cause the MOSFET to go from the saturation to the active region when  $I_D = 0.2$ mA?



## <u>Solution</u>

a.) Let us solve for the value of  $V_{GS}$  that gives  $I_D = 0.2$ mA when the MOSFET is saturated.

$$I_D = 0.5K_n (V_{GS} - V_{TN})^2 = 0.5(V_{GS} - 1)^2 = 0.2$$
  

$$0.4 = V_{GS}^2 - 2V_{GS} + 1 \qquad \Rightarrow \qquad V_{GS}^2 - 2V_{GS} + 0.6 = 0$$
  

$$V_{GS} = 1 \pm 0.5\sqrt{4 - 0.6(4)} = 1 \pm 0.5\sqrt{1.6} = 1 \pm 0.632V \qquad \Rightarrow \qquad V_{GS} = 1.632V (2)$$

Since we know that  $V_G = 5V(1)$ , then  $V_S = 5 - 1.632 = 3.367V$ 

Therefore, 
$$R_S = \frac{V_S}{I_D} = \frac{3.367}{0.2\text{mA}} = \underline{16.84\text{k}\Omega}$$
 (3)

b.) To find the value of *RD* that will cause the MOSFET to leave the saturation region and enter the active region, we will use the following relationship that gives the conditions at the boundary of the two regions.

$$V_{DS} = V_{GS} - V_{TN} \quad (1)$$

This relationship can be rewritten as,

$$V_D - V_S = V_G - V_S - V_{TN} \rightarrow V_D = V_G - V_{TN} = V_G - 1$$
 (1)

Therefore,  $V_D = 5 \cdot 1 = 4$ V is when the MOSFET will be at the boundary of the two regions. Thus, the voltage drop across  $R_D$  is 6V and the current through it is 0.2mA. From Ohm's law, we get,

$$R_D = \frac{(10 - V_D)}{I_D} = \frac{6V}{0.2\text{mA}} = \underline{30k\Omega}$$
 (2)

#### Problem 5

The following questions give the dc voltages at the terminals of an active device. You are to calculate the designated dc current.

a.) Find the diode current,  $I_D$ , where  $I_S = 100$  fA and  $V_T = 0.025$ V (2 pts).

Obviously, the diode is forward biased. Therefore,

$$I_D = I_S \exp\left(\frac{V_D}{V_T}\right) = 10^{-13} \exp\left(\frac{0.6}{0.025}\right) = \underline{2.65 \text{ mA}}$$

b.) Find the drain-source current,  $I_{DS}$ , where  $K_n' = 25\mu A/V^2$ ,  $V_{TN} = 1V$  and W/L = 10 (2 pts).

We see that the enhancement, n-channel MOSFET is in the saturation region. Therefore,

$$I_{DS} = \frac{K_n'W}{2L} (V_{GS} - V_{TN})^2 = \frac{25 \cdot 10}{2} (2 - 1)^2 = \underline{125 \ \mu A}$$

c.) Find the collector, emitter, and base currents,  $I_C$ ,  $I_E$ , and  $I_B$  if  $I_S = 100$ fA,  $V_T = 0.025$ V and  $\beta_F = 100$  (4 pts).

We see that the npn BJT is in the forward active region. Therefore,

$$I_{C} = I_{S} \exp\left(\frac{V_{BE}}{V_{T}}\right) = 10^{-13} \exp\left(\frac{0.7}{0.025}\right) = \underline{144.6 \text{ mA}}$$
$$I_{B} = \frac{I_{C}}{\beta_{F}} = \underline{1.446 \text{ mA}} \qquad \text{and} \qquad I_{E} = I_{C} + I_{B} = \underline{146 \text{ mA}}$$

d.) Repeat (b.) if  $V_D = 1$  V and  $V_G = 3$  V (2 pts).

We see that the enhancement, n-channel MOSFET is in the linear region. Therefore,

$$I_{DS} = K_n \frac{W}{L} \left( V_{GS} - V_{TN} - \frac{V_{DS}}{2} \right) V_{DS} = 25 \cdot 10(3 - 1 - 0.5)(1) = \underline{375 \ \mu A}$$



$$0.7V \xrightarrow{I_B} V_{IC}$$