Homework Assignment No. 1 – Solutions

Problem 1

(a.) The first thing to do is to find Thevenin's equivalent circuit seen from the diode.

The Thevenin voltage is,

$$V_{TH} = V_{IN} \left(\frac{2}{3} - \frac{1}{3}\right) = \frac{V_{IN}}{3}$$

The Thevenin resistance is,

$$R_{TH} = 1k\Omega ||2k\Omega + 1k\Omega ||2k\Omega = \frac{4}{3} k\Omega$$

The equivalent circuit now becomes,

Now , with $V_{IN} = 10$ V, we know the diode is forward biased. Therefore, replacing it with a short-circuit gives,

$$V_D = \underline{0V}$$
 and $I_D = \frac{10}{3} x \frac{3}{4k\Omega} = \underline{2.5 \text{ mA}}$

(b.) With V_{IN} = -10V, we know the diode is reverse biased. Therefore replacing it with an open-circuit gives,

$$V_D = -3.33 \text{V}$$
 and $I_D = 0 \text{ mA}$





Problem 2

An enhancement NMOS amplifier is shown. The following questions are independent of each other (i.e. the answer of one is *not* used in the next question).

(a.) If
$$I_D = 0.5$$
mA, $V_T = 1$ V, and $K = 0.5$ mA/V, find g_m .

(b.) If $g_m = 0.5$ mA/V and $r_o = \infty$, find an algebraic expression for R_{out} and $A_v = v_{out}/v_{in}$.



(c.) Design R_D and R_S to give $R_{out} = 10k\Omega$ and $A_v = -10V/V$ if $g_m = 2mA/V$ and $r_o = \infty$.

<u>Solution</u>

a.)
$$g_m = \sqrt{2KI_D} = \sqrt{2.500.500} \,\mu\text{A} = 707\mu\text{S} = 0.707\text{mS}$$

b.) The corresponding small-signal model:

$$\frac{v_{out}}{v_{in}} = \frac{v_{out}}{v_{gs}} \frac{v_{gs}}{v_{in}}$$

$$\frac{v_{out}}{v_{gs}} = -g_m(R_D || R_L)$$

$$v_{gs} = v_g - v_s = v_{in} - (g_m R_S v_{gs})$$
which gives
$$\frac{v_{gs}}{v_{in}} = \frac{1}{1 + g_m R_S} \rightarrow \frac{v_{out}}{v_{gs}} = \frac{\frac{-g_m(R_D || R_L)}{1 + g_m R_S}}{1 + g_m R_S} \text{ and } R_{out} = \frac{R_D || R_L}{R_D || R_L}$$
c.)
$$R_{out} = 10k\Omega = R_D || R_L = R_D || 20k\Omega \rightarrow R_D = \frac{20k\Omega}{1 + g_m R_S} = \frac{-20}{1 + \frac{R_S}{500}} \rightarrow R_S = \frac{500\Omega}{1 + g_m R_S}$$

A pnp BJT circuit is shown. (a.) Find the dc values of I_E , I_C , I_B , V_E , V_C and V_B if $\beta = 50$ and $V_{EB}(\text{on}) = 0.65\text{V}$. (b.) For what value of R_C does the BJT become saturated? (Recall that saturation of a BJT corresponds to the *BE* and *BC* junctions forward biased.) <u>Solution</u>



(b.) Saturation occurs when $V_{BC} = 0$ of $V_B = V_C$. Therefore, $V_C = 1.96$ V. The current through R_C is still 0.98mA, so solving for R_C gives,

$$R_C = \frac{V_C + 10V}{I_C} = \frac{11.96V}{0.98\text{mA}} = 12.20\text{k}\Omega \implies \boxed{R_C = 12.2\text{k}\Omega}$$



1mA

o V_E

 V_B

+10V

Problem 4

For the transistor shown, $\beta = 100$, $r_{\pi} = 2.5k\Omega$, and $g_m = 0.04S$. Draw the small signal model and find the numerical values of the small signal voltage gain, v_{out}/v_{in} , the input resistance, R_{in} , and the output resistance, R_{out} .

<u>Solution</u>

Small-signal model:



 R_{in}

10V

 $R_L =$

 $10\bar{k}\Omega$

 $R_C = 5k\Omega$

R_{out}

Problem 5

The following questions give the dc voltages at the terminals of an active device. You are to calculate the designated dc current.

a.) Find the diode current, I_D , where $I_S = 100$ fA and $V_T = 0.025$ V (2 pts).

Obviously, the diode is forward biased. Therefore,

$$I_D = I_S \exp\left(\frac{V_D}{V_T}\right) = 10^{-13} \exp\left(\frac{0.6}{0.025}\right) = \underline{2.65 \text{ mA}}$$

b.) Find the drain-source current, I_{DS} , where $K_n' = 25\mu A/V^2$, $V_{TN} = 1V$ and W/L = 10 (2 pts).

We see that the enhancement, n-channel MOSFET is in the saturation region. Therefore,

$$I_{DS} = \frac{K_n W}{2L} (V_{GS} - V_{TN})^2 = \frac{25 \cdot 10}{2} (2 - 1)^2 = \frac{125 \,\mu\text{A}}{2}$$

c.) Find the collector, emitter, and base currents, I_C , I_E , and I_B if $I_S = 100$ fA, $V_T = 0.025$ V and $\beta_F = 100$ (4 pts).

We see that the npn BJT is in the forward active region. Therefore,

$$I_{C} = I_{S} \exp\left(\frac{V_{BE}}{V_{T}}\right) = 10^{-13} \exp\left(\frac{0.7}{0.025}\right) = \underline{144.6 \text{ mA}}$$
$$I_{B} = \frac{I_{C}}{\beta_{F}} = \underline{1.446 \text{ mA}} \qquad \text{and} \qquad I_{E} = I_{C} + I_{B} = \underline{146 \text{ mA}}$$

d.) Repeat (b.) if $V_D = 1$ V and $V_G = 3$ V (2 pts).

We see that the enhancement, n-channel MOSFET is in the linear region. Therefore,

$$I_{DS} = K_n \frac{W}{L} \left(V_{GS} - V_{TN} - \frac{V_{DS}}{2} \right) V_{DS} = 25 \cdot 10(3 - 1 - 0.5)(1) = \underline{375 \ \mu A}$$





F02Q01P1C

0.7V ō