

COMPLEX CMOS GATES

Example: $F = \overline{(A+B)} \cdot C$

1) De Morgan's Law

$$\overline{(a+b)} = \bar{a} \cdot \bar{b}$$

$$\overline{a \cdot b} = \bar{a} + \bar{b}$$

Duality

$$a+b \Leftrightarrow \overline{a \cdot \bar{b}}$$

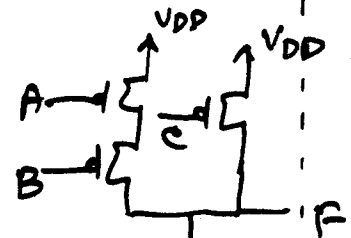
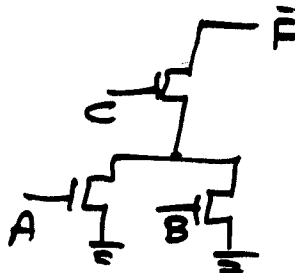
$$(a+b) \cdot c \Leftrightarrow \overline{\bar{a} \cdot \bar{b} \cdot \bar{c}}$$

2) AND in CMOS \rightarrow series NMOS, parallel PMOS
 OR \rightarrow parallel NMOS, series PMOS

\rightarrow 3) Since NMOS act to pull F low, implement \bar{F} .

\rightarrow 4) " PMOS act to pull F high, " \bar{F} but with inverted inputs

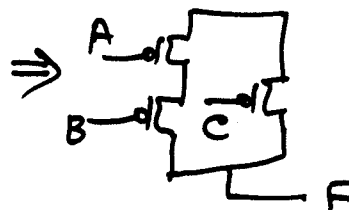
$$F = \overline{(A+B)} \cdot C \rightarrow \bar{F} = (A+B) \cdot \bar{C}$$



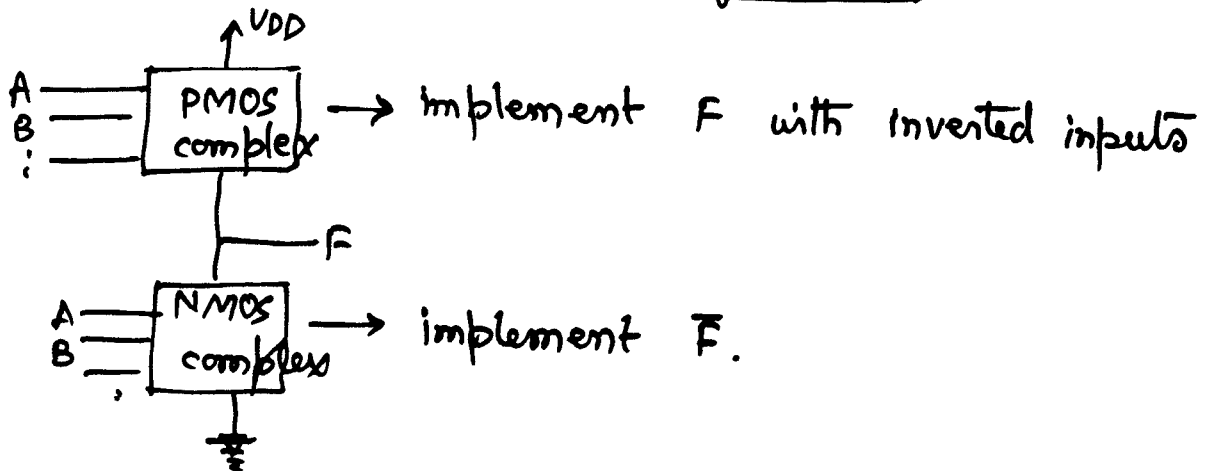
$$F = \overline{(A+B)} \cdot C = \bar{A} \cdot \bar{B} + \bar{C}$$

$$= \overline{(A+B)} + \bar{C}$$

$$F = \bar{A} \cdot \bar{B} + \bar{C} = A \cdot B + C$$



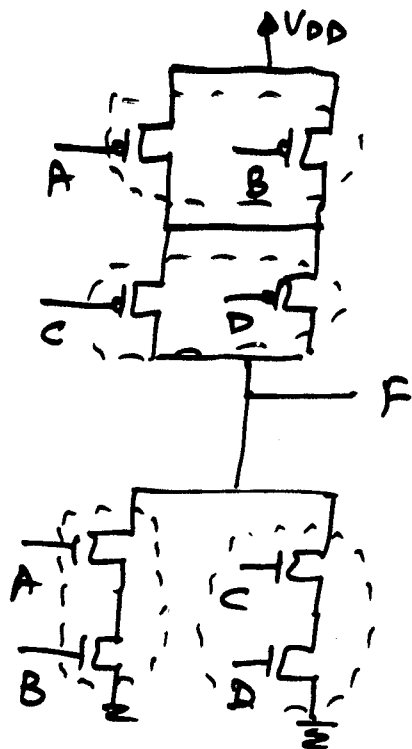
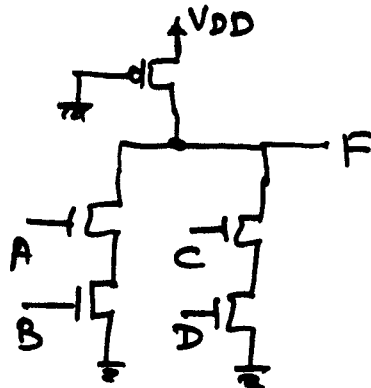
Generalized complex gate synthesis



Ex. 5.3

$F = \overline{A \cdot B + C \cdot D}$ as a single-stage CMOS and Pseudo-NMOS

$$\bar{F} = A \cdot B + C \cdot D$$



$$F = \overline{A \cdot B + C \cdot D}$$

$$F = \overline{\bar{A} \cdot \bar{B} + \bar{C} \cdot \bar{D}}$$

$$= (\underbrace{A+B}) \cdot (\underbrace{C+D})$$

Ex. XOR gate

$$F_{\text{XOR}} = a\bar{b} + \bar{a}b$$

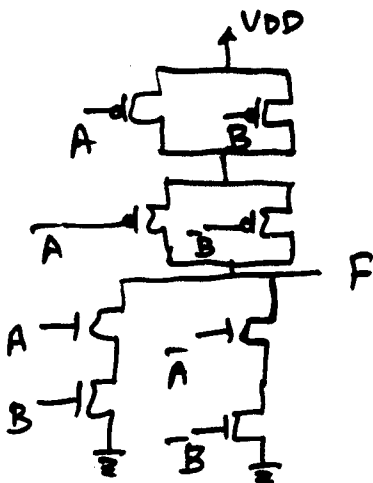
$$\bar{F}_{\text{XOR}} = \overline{a\bar{b} + \bar{a}b}$$

$$= \overline{(a\bar{b}) \cdot (\bar{a}b)}$$

$$= (\bar{a} + b) \cdot (a + \bar{b})$$

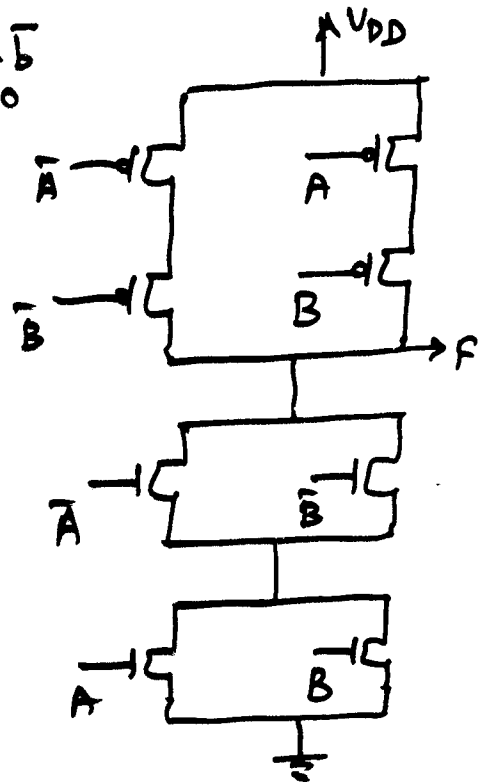
$$= \underbrace{\bar{a}a}_{=0} + a\bar{b} + \bar{a}b + \underbrace{b\bar{b}}_{=0}$$

$$\bar{F}_{\text{XOR}} = a\bar{b} + \bar{a}b$$

XNOR gate

$$F_{\text{XNOR}} = ab + \bar{a}\bar{b}$$

$$\begin{aligned} F_{\text{XNOR}} &= \bar{a}\bar{b} + \bar{\bar{a}\bar{b}} \\ &= \bar{a}\bar{b} + a\bar{b} \end{aligned}$$



$$F = (A+B) \cdot (\bar{A} + \bar{B})$$

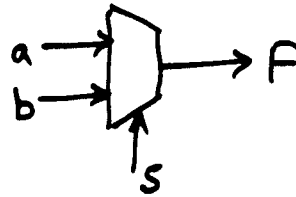
$$F = \overline{(A+B) \cdot (\bar{A} + \bar{B})}$$

$$= \overline{(A+B)} + \overline{(\bar{A} + \bar{B})}$$

$$= \bar{A}\bar{B} + A\bar{B}$$

Ex. Multiplexer

$$\underline{F = a \cdot s + b \bar{s}}$$



$$\bar{F} = \overline{(a \cdot s + b \cdot \bar{s})}$$

$$= \overline{(a \cdot s)} \cdot \overline{(b \cdot \bar{s})}$$

~~$$= (a \cdot \bar{s}) + (b \cdot s)$$~~

$$F = \bar{a} \cdot \bar{s} + \bar{b} \cdot s \xrightarrow{\text{PMOS}}$$

