Lecture 130 – Compensation of Op Amps-II (1/26/04)

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LECTURE 130 – COMPENSATION OF OP AMPS-II (READING: GHLM – 638-652, AH – 260-269)

INTRODUCTION

The objective of this presentation is to continue the ideas of the last lecture on compensation of op amps.

Outline

- Compensation of Op Amps General principles Miller, Nulling Miller Self-compensation Feedforward
- Summary

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Conditions for Stability of the Two-Stage Op Amp (Assuming $p_3 \ge GB$)

• Unity-gainbandwith is given as:

$$GB = A_{\mathcal{V}}(0) \cdot |p_1| = \left(\frac{gmIgmIIRIRII}{gmIIRIRIIC_c}\right) = \frac{gmI}{C_c} = \left(\frac{gm1gm2R_1R_2}{gm2R_1R_2C_c}\right) = \frac{gm1}{C_c}$$

• The requirement for 45° phase margin is:

$$\pm 180^{\circ} - \operatorname{Arg}[AF] = \pm 180^{\circ} - \tan^{-1}\left(\frac{\omega}{|p_1|}\right) - \tan^{-1}\left(\frac{\omega}{|p_2|}\right) - \tan^{-1}\left(\frac{\omega}{z}\right) = 45^{\circ}$$

Let $\omega = GB$ and assume that $z \ge 10GB$, therefore we get,

$$\pm 180^{\circ} - \tan^{-1}\left(\frac{GB}{|p_{1}|}\right) - \tan^{-1}\left(\frac{GB}{|p_{2}|}\right) - \tan^{-1}\left(\frac{GB}{z}\right) = 45^{\circ}$$

$$135^{\circ} \approx \tan^{-1}(A_{\nu}(0)) + \tan^{-1}\left(\frac{GB}{|p_{2}|}\right) + \tan^{-1}(0.1) = 90^{\circ} + \tan^{-1}\left(\frac{GB}{|p_{2}|}\right) + 5.7^{\circ}$$

$$39.3^{\circ} \approx \tan^{-1}\left(\frac{GB}{|p_{2}|}\right) \Rightarrow \frac{GB}{|p_{2}|} = 0.818 \Rightarrow \boxed{|p_{2}| \ge 1.22GB}$$

• The requirement for 60° phase margin:

 $|p_2| \ge 2.2GB$ if $z \ge 10GB$

• If 60° phase margin is required, then the following relationships apply:

$$\frac{g_{m6}}{C_c} > \frac{10g_{m1}}{C_c} \implies \boxed{g_{m6} > 10g_{m1}} \quad \text{and} \quad \frac{g_{m6}}{C_2} > \frac{2.2g_{m1}}{C_c} \implies \boxed{C_c > 0.22C_2}$$

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Why is the RHP zero a problem?

Because it boosts the magnitude but lags the phase - the worst possible combination for stability.



Use of Buffer with Finite Output Resistance to Eliminate the RHP Zero

Assume that the unity-gain buffer has an output resistance of R_o . Model:



It can be shown that if the output resistance of the buffer amplifier, R_o , is not neglected that another pole occurs at,

$$p_4 \cong \frac{-1}{R_o[C_I C_c / (C_I + C_c)]}$$

and a LHP zero at

$$z_2 \cong \frac{-1}{R_o C_c}$$

Closer examination shows that if a resistor, called a *nulling resistor*, is placed in series with C_c that the RHP zero can be eliminated or moved to the LHP.

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Use of Nulling Resistor to Eliminate the RHP Zero (or turn it into a LHP zero)[†]



Nodal equations:

$$g_{mI}V_{\text{in}} + \frac{V_I}{R_I} + sC_IV_I + \left(\frac{sC_c}{1+sC_cR_z}\right)(V_I - V_{out}) = 0$$
$$g_{mII}V_I + \frac{V_o}{R_{II}} + sC_{II}V_{out} + \left(\frac{sC_c}{1+sC_cR_z}\right)(V_{out} - V_I) = 0$$

Solution:

$$\frac{V_{out}(s)}{V_{in}(s)} = \frac{a\{1 - s[(C_c/g_{mII}) - R_zC_c]\}}{1 + bs + cs^2 + ds^3}$$

where

$$\begin{aligned} a &= g_{mI}g_{mII}R_{I}R_{II} \\ b &= (C_{II} + C_{c})R_{II} + (C_{I} + C_{c})R_{I} + g_{mII}R_{I}R_{II}C_{c} + R_{z}C_{c} \\ c &= [R_{I}R_{II}(C_{I}C_{II} + C_{c}C_{I} + C_{c}C_{II}) + R_{z}C_{c}(R_{I}C_{I} + R_{II}C_{II})] \\ d &= R_{I}R_{II}R_{z}C_{I}C_{II}C_{c} \end{aligned}$$

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 ^{*} W.J. Parrish, "An Ion Implanted CMOS Amplifier for High Performance Active Filters", Ph.D. Dissertation, 1976, Univ. of CA., Santa Barbara.
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Use of Nulling Resistor to Eliminate the RHP - Continued

If R_z is assumed to be less than R_I or R_{II} and the poles widely spaced, then the roots of the above transfer function can be approximated as

$$p_{1} \approx \frac{-1}{(1 + g_{mII}R_{II})R_{I}C_{c}} \approx \frac{-1}{g_{mII}R_{II}R_{I}C_{c}}$$

$$p_{2} \approx \frac{-g_{mII}C_{c}}{C_{I}C_{II} + C_{c}C_{I} + C_{c}C_{II}} \approx \frac{-g_{mII}}{C_{II}}$$

$$p_{4} = \frac{-1}{R_{z}C_{I}} \qquad (p_{3} \text{ has been used previously for the mirror pole so we choose } p_{4} \text{ for the nulling resistor pole})$$

and

$$z_1 = \frac{1}{C_c(1/g_{mII} - R_z)}$$

Note that the zero can be placed anywhere on the real axis.

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Conceptual Illustration of the Nulling Resistor Approach



The output voltage, V_{out} , can be written as

$$V_{out} = \frac{-g_{m6}R_{II}\left(R_z + \frac{1}{sC_c}\right)}{R_{II} + R_z + \frac{1}{sC_c}}V' + \frac{R_{II}}{R_{II} + R_z + \frac{1}{sC_c}}V'' = \frac{-R_{II}\left[g_{m6}R_z + \frac{g_{m6}}{sC_c} - 1\right]}{R_{II} + R_z + \frac{1}{sC_c}}V$$

when V = V' = V''.

Setting the numerator equal to zero and assuming $g_{m6} = g_{mII}$ gives,

$$z_1 = \frac{1}{C_c(1/g_{mII} - R_z)}$$

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A Design Procedure that Allows the RHP Zero to Cancel the Output Pole, p₂

We desire that $z_1 = p_2$ in terms of the previous notation. Therefore,

$$\frac{1}{C_c(1/g_{mII} - R_z)} = \frac{-g_{mII}}{C_{II}} \xrightarrow{P_4} \frac{j\omega}{P_2} \xrightarrow{p_1} \sigma$$

The value of R_z c

$$R_z = \left(\frac{C_c + C_{II}}{C_c}\right) (1/g_{mII})$$

With p_2 canceled, the remaining roots are p_1 and p_4 (the pole due to R_z). For unity-gain stability, all that is required is that

$$|p_4| > A_v(0)|p_1| = \frac{A_v(0)}{g_{mII}R_{II}R_IC_c} = \frac{g_{mI}}{C_c}$$

and

 $(1/R_z C_I) > (g_{mI}/C_c) = GB$ Substituting R_z into the above inequality and assuming $C_{II} >> C_c$ results in

$$C_c > \sqrt{\frac{g_{mI}}{g_{mII}}} C_I C_{II}$$

This procedure gives excellent stability for a fixed value of $C_{II} (\approx C_L)$. Unfortunately, as C_L changes, p_2 changes and the zero must be readjusted to cancel p_2 .

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Increasing the Magnitude of the Output Pole[†]

The magnitude of the output pole, p_2 , can be increased by introducing gain in the Miller capacitor feedback path. For example,



The resistors R_1 and R_2 are defined as

$$R_1 = \frac{1}{g_{ds2} + g_{ds4} + g_{ds9}}$$
 and $R_2 = \frac{1}{g_{ds6} + g_{ds7}}$

where transistors M2 and M4 are the output transistors of the first stage. Nodal equations:

$$I_{in} = G_1 V_1 - g_{m8} V_{s8} = G_1 V_1 - \left(\frac{g_{m8} s C_c}{g_{m8} + s C_c}\right) V_{out} \quad \text{and} \quad 0 = g_{m6} V_1 + \left[G_2 + s C_2 + \frac{g_{m8} s C_c}{g_{m8} + s C_c}\right] V_{out}$$

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B.K. Ahuja, "An Improved Frequency Compensation Technique for CMOS Operational Amplifiers," IEEE J. of Solid-State Circuits, Vol. SC-18, No. 6 (Dec. 1983) pp. 629-633.

Increasing the Magnitude of the Output Pole - Continued

Solving for the transfer function V_{out}/I_{in} gives,

$$\frac{V_{out}}{I_{in}} = \left(\frac{-g_{m6}}{G_1 G_2}\right) \left[\frac{\left(1 + \frac{sC_c}{g_{m8}}\right)}{1 + s\left[\frac{C_c}{g_{m8}} + \frac{C_2}{G_2} + \frac{C_c}{G_2} + \frac{g_{m6}C_c}{G_1 G_2}\right] + s^2 \left(\frac{C_c C_2}{g_{m8} G_2}\right)} \right]$$

Using the approximate method of solving for the roots of the denominator gives

$$p_1 = \frac{-1}{\frac{C_c}{g_{m8}} + \frac{C_c}{G_2} + \frac{C_2}{G_2} + \frac{g_{m6}C_c}{G_1G_2}} \approx \frac{-6}{g_{m6}r_{ds}^2C_c}$$

and

$$p_{2} \approx \frac{-\frac{g_{m6}r_{ds}^{2}C_{c}}{6}}{\frac{C_{c}C_{2}}{g_{m8}G_{2}}} = \frac{g_{m8}r_{ds}^{2}G_{2}}{6} \left(\frac{g_{m6}}{C_{2}}\right) = \left(\frac{g_{m8}r_{ds}}{3}\right) |p_{2}'|$$

where all the various channel resistance have been assumed to equal r_{ds} and p_2 ' is the output pole for normal Miller compensation.

Result:

Dominant pole is approximately the same and the output pole is increased by $\approx g_m r_{ds}$.

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Concept Behind the Increasing of the Magnitude of the Output Pole



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Self compensation occurs when the load capacitor is the compensation capacitor (can never be unstable for resistive feedback)



SUMMARY

Compensation

- Designed so that the op amp with unity gain feedback (buffer) is stable
- Types
 - Miller
 - Miller with nulling resistors
 - Self Compensating
 - Feedforward

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