LECTURE 040 – COMMON SOURCE AND EMITTER OUTPUT STAGES

(READING: GHLM – 384-398, AH – 218-221)

Objective
The objective of this presentation is:
Show how to design stages that
1.) Provide sufficient output power in the form of voltage or current.
2.) Avoid signal distortion.
3.) Be efficient
4.) Provide protection from abnormal conditions (short circuit, over temperature, etc.)

Outline
• Common source stage
• Common emitter stage
• Summary
COMMON SOURCE OUTPUT STAGE

Current source load inverter

A Class A circuit has current flow in the MOSFETs during the entire period of a sinusoidal signal.

Characteristics of Class A amplifiers:
- Unsymmetrical sinking and sourcing
- Linear
- Poor efficiency

Efficiency = \( \frac{P_{RL}}{P_{Supply}} = \frac{v_{OUT}(\text{peak})^2}{2RL} \frac{1}{(V_{DD}-V_{SS})I_Q} = \frac{v_{OUT}(\text{peak})^2}{2RL} \frac{1}{(V_{DD}-V_{SS})} \)\( \left( \frac{V_{DD}-V_{SS}}{2RL} \right) = \left( \frac{v_{OUT}(\text{peak})}{V_{DD}-V_{SS}} \right)^2 \)

Maximum efficiency occurs when \( v_{OUT}(\text{peak}) = V_{DD} = |V_{SS}| \) which gives 25%.
**Specifying the Performance of a Common Source Amplifier**

Output resistance:

\[ r_{out} = \frac{1}{g_{ds1} + g_{ds2}} = \frac{1}{(\lambda_1 + \lambda_2)I_D} \]

Current:

- Maximum sinking current is,

\[ I_{\text{OUT}}^- = \frac{K'_{1W1}}{2L_1} (V_{DD} - V_{SS} - V_{T1})^2 - I_Q \]

- Maximum sourcing current is,

\[ I_{\text{OUT}}^+ = \frac{K'_{2W2}}{2L_2} (V_{DD} - V_{GG2} - |V_{T2}|)^2 \leq I_Q \]

Requirements:

- Want \( r_{out} \ll R_L \)
- \( |I_{\text{OUT}}^-| > C_L \cdot SR \)
- \( |I_{\text{OUT}}^-| > \frac{v_{\text{OUT}}(\text{peak})}{R_L} \)

The maximum current will be determined by **both** the current required to provide the necessary slew rate (\( C_L \)) and the current required to provide a voltage across the load resistor (\( R_L \)).
Small-Signal Performance of the Class A Amplifier

Although we have considered the small-signal performance of the Class A amplifier as the current source load inverter, let us include the influence of the load.

The modified small-signal model:

\[ \frac{v_{out}}{v_{in}} = \frac{-g_{m1}}{g_{ds1} + g_{ds2} + G_L} \]

The small-signal frequency response includes:

A zero at

\[ z = \frac{g_{m1}}{C_{gd1}} \]

and a pole at

\[ p = \frac{-(g_{ds1} + g_{ds2} + G_L)}{C_{gd1} + C_{gd2} + C_{bd1} + C_{bd2} + C_L} \]
Example 5.5-1 - Design of a Simple Class-A Output Stage

Use the values of $K_{N} = 110 \mu A/V^2$, $K_P = 50 \mu A/V^2$, $V_{TN} = 0.7 V$ and $V_{TP} = -0.7 V$ and design the $W/L$ ratios of M1 and M2 so that a voltage swing of ±2 volts and a slew rate of ±1 volt/µs is achieved if $R_L = 20 \ k\Omega$ and $C_L = 1000 \ pF$. Assume that $V_{DD} = |V_{SS}| = 3 \ volts$ and $V_{GG2} = 0 \ volts$. Let the channel lengths be 2 µm and assume that $C_{gd1} = 100fF$.

Solution

Let us first consider the effects of $R_L$ and $C_L$.

$$i_{OUT}(\text{peak}) = \frac{\pm 2V}{20k\Omega} = \pm 100 \mu A \quad \text{and} \quad C_L \cdot SR = 10^{-9} \cdot 10^6 = 1000 \mu A$$

Since the slew rate current $>>$ the current for $R_L$, we can safely assume that all of the current supplied by the inverter is available to charge $C_L$.

Using a value of ±1 mA,

$$\frac{W_1}{L_1} = \frac{2(I_{OUT} + I_Q)}{K_{N}(V_{DD} + |V_{SS}| - V_{TN})^2} = \frac{4000}{110 \cdot (5.3)^2} \approx 3 \mu m \quad 2 \mu m$$

and

$$\frac{W_2}{L_2} = \frac{2I_{OUT}^+}{K_P(V_{DD} - V_{GG2} - |V_{TP}|)^2} = \frac{2000}{50 \cdot (2.3)^2} \approx 15 \mu m \quad 2 \mu m$$

The small-signal performance of this amplifier is, $A_V = -8.21 \ V/V$ (includes $R_L = 20k\Omega$)
**Broadband Harmonic Distortion**

The linearity of an amplifier can be characterized by its influence on a pure sinusoidal input signal.

Assume the input is,

\[ V_{\text{in}}(\omega) = V_p \sin(\omega t) \]

The output of an amplifier with distortion will be

\[ V_{\text{out}}(\omega) = a_1 V_p \sin(\omega t) + a_2 V_p \sin(2\omega t) + \cdots + a_n V_p \sin(n\omega t) \]

**Harmonic distortion (HD)** for the \( i \)th harmonic can be defined as the ratio of the magnitude of the \( i \)th harmonic to the magnitude of the fundamental.

For example, second-harmonic distortion would be given as

\[ HD_2 = \frac{a_2}{a_1} \]

**Total harmonic distortion (THD)** is defined as the square root of the ratio of the sum of all of the second and higher harmonics to the magnitude of the first or fundamental harmonic.

Thus, \( THD \) can be expressed as

\[ THD = \frac{[a_2^2 + a_3^2 + \cdots + a_n^2]^{1/2}}{a_1} \]

The distortion of the class A amplifier is good for small signals and becomes poor at maximum output swings because of the nonlinearity of the voltage transfer curve for large-signal swing.
COMMON EMITTER OUTPUT STAGE

Common Emitter Class A Output Stage

Large signal characteristic:

\[ i_{OUT} = I_Q - i_{C1}, \quad v_{OUT} = i_{OUT} R_L, \quad \text{and} \quad i_{C1} = I_s1 \exp\left(\frac{v_{IN}}{V_t}\right) \]

\[ \therefore \quad v_{OUT} = -R_L \left[ I_s1 \exp\left(\frac{v_{IN}}{V_t}\right) - I_Q \right] \]
Harmonic Distortion in the Common Emitter Output Stage

Assume the input signal is

\[ v_{IN} = V_{BE1} + v_{in} \]

Substituting this in the expression on the last slide gives,

\[ v_{OUT} = -R_L \left[ I_s 1 \exp \left( \frac{v_{IN}}{V_t} \right) - I_Q \right] = - R_L \left[ I_s 1 \exp \left( \frac{V_{BE1}}{V_t} \right) \exp \left( \frac{v_{in}}{V_t} \right) - I_Q \right] = - I_Q R_L \left[ \exp \left( \frac{v_{in}}{V_t} \right) - 1 \right] \]

Using the expansion of \( \exp(x) \approx 1 + x + x^2/2 + x^3/6 + \cdots \) gives

\[ v_{OUT} = - I_Q R_L \left[ \frac{v_{in}}{V_t} + \frac{1}{2} \left( \frac{v_{in}}{V_t} \right)^2 + \frac{1}{6} \left( \frac{v_{in}}{V_t} \right)^3 + \cdots \right] = a_1 v_{in} + a_2 v_{in}^2 + a_3 v_{in}^3 + \cdots \]

where

\[ a_1 = - \frac{I_Q R_L}{V_t}, \quad a_2 = - \frac{I_Q R_L}{2 V_t^2} \quad \text{and} \quad a_3 = - \frac{I_Q R_L}{6 V_t^3} \]

Suppose \( v_{in}(t) = V_p \sin \omega t \), then

\[ v_{OUT}(t) = a_1 V_p \sin \omega t + a_2 V_p^2 \sin^2 \omega t + a_3 V_p^3 \sin^3 \omega t + \cdots \]

\[ = a_1 V_p \sin \omega t + \frac{a_2 V_p^2}{2} (1 - \cos 2\omega t) + \frac{a_3 V_p^3}{4} (3 \sin \omega t - \sin 3 \omega t) + \cdots \]

\[ \therefore HD_2 = \frac{a_2 V_p^2}{2} \frac{1}{a_1 V_p} = \frac{a_2 V_p}{2a_1} = \frac{V_p}{4 V_t} \quad \text{and} \quad HD_3 = \frac{a_3 V_p^3}{4} \frac{1}{a_1 V_p} = \frac{a_3 V_p^2}{4 a_1} = \frac{1}{24} \left( \frac{V_p}{V_t} \right)^2 \]

For \( V_p = 0.5 V_t \), \( HD_2 = 12.5\% \) and \( HD_2 \approx 1\% \).
Small Signal Performance of the Common Emitter Output Stage

Let $r_{o1}||r_{o2} = r_o$, then

$$R_{in} = r_{\pi1} = \frac{\beta_o}{g_m1}, \quad R_{out} = \frac{r_oR_L}{r_o + R_L} \approx R_L, \quad \frac{v_{out}}{v_{in}} = \frac{-g_m1r_oR_L}{r_o + R_L} \approx -g_m1R_L \quad \text{and} \quad \frac{i_{out}}{i_{in}} = \frac{\beta_o r_o}{r_o + R_L}$$

If $V_{out}(peak) = 0.6V$, $R_L = 1k\Omega$ and $I_Q = 1.86mA$, then

$$A_v \approx -g_m1R_L = -\frac{I_C}{V_t} R_L = -\frac{1.86}{26} 1000 = -70.6V/V \quad \Rightarrow \quad V_P = \frac{0.6}{\left|A_v\right|} = \frac{0.6}{70.6} = 8.5mV \text{ (peak)}$$

$$HD_2 = \frac{1}{4} \frac{18.5}{26} = 0.082 \quad \text{and} \quad HD_3 = \frac{1}{24} \left(\frac{8.5}{26}\right)^2 = 0.0045$$

Where does the distortion come from?

The ac gain at the negative peak output voltage is $-\frac{1.86+0.6}{26} 1000 = -94.6V/V$

The ac gain at the positive peak output voltage is $-\frac{1.86-0.6}{26} 1000 = -48.5V/V$

Note the emitter follower is much more linear because of the inherent negative feedback.
SUMMARY

Requirements of Output Stages

• The objectives are to provide output power in form of voltage and/or current.
• In addition, the output amplifier should be linear and be efficient.
• Low output resistance is required to provide power efficiently to a small load resistance.
• High source/sink currents are required to provide sufficient output voltage rate due to large load capacitances.
• Types of output stages considered:
  - Common emitter and common source
• Maximum efficiency is 25%
• Second-harmonic distortion can be significant