

CHAPTER 7

7.1

(a) Transistor parameters are

$$r_{\pi} = \frac{\beta_o}{g_m} = 200 \times 52 = 10.4 \text{ k}\Omega$$

$$\tau_T = \frac{1}{2\pi f_T} = 318 \text{ ps}$$

$$C_{\pi} + C_{\mu} = g_m \tau_T = \frac{1}{52} \times 318 = 6.12 \text{ pF}$$

$$\therefore C_{\pi} = 6.1 - 0.3 = 5.8 \text{ pF}$$

$$C_M = (1 + g_m R_L) C_{\mu} \\ = \left(1 + \frac{3000}{52}\right) \times 0.3 = 17.6 \text{ pF}$$

In (7.12) and (7.9)

$$f_{-3dB} = \frac{1}{2\pi} \frac{5000 + 300 + 10400}{(5000 + 300) \times 10400} \frac{10^{12}}{5.8 + 17.6} \\ = 1.94 \text{ MHz}$$

(b) From (7.27)

$$P_2 = -\left(\frac{1}{R_L C_{\mu}} + \frac{1}{R C_{\pi}} + \frac{1}{R_L C_{\pi}} + \omega_T\right)$$

$$R = (R_S + r_b) \parallel r_{\pi} \\ = 5300 \parallel 10400 = 3511 \Omega$$

$$\therefore P_2 = -\left(\frac{10^{12}}{3000 \times 0.3} + \frac{10^{12}}{3511 \times 5.8} + \frac{10^{12}}{3000 \times 5.8} + 2\pi \times 500 \times 10^6\right) \\ = -(11.1 + 0.49 + 0.57 + 31.4) \times 10^8 \text{ rad/sec} \\ = -43.6 \times 10^8 \text{ rad/sec} \\ = -693 \text{ MHz}$$

COMMON EMITTER GAIN STAGE

VCC 1 0 5V
 RL 1 2 3K
 Q1 2 3 0 NPN
 RS 4 3 5K
 VI 4 0 0.7696 AC
 .TF V(2) VI
 .PLOT AC VDB(2)
 .PLOT AC VP(2)
 .AC DEC 10 100K 1GIG
 .MODEL NPN NPN IS=1E-16A BF=200
 + RB=300 CJC=0.3PF CJS=0 TP=302PS
 * ASSUME CJE SMALL COMPARED TO CB
 .OPTIONS NOPAGE NOMOD
 .WIDTH OUT=80
 .OPTIONS SPICE
 .OP
 .END

***** OPERATING POINT INFORMATION TNOM= 27.000 TEMP= 27.000

+0:1 = 5.000E+00 0:2 = 3.497E+00 0:3 = 7.571E-01
 +0:4 = 7.696E-01

**** BIPOLAR JUNCTION TRANSISTORS

ELEMENT 0:Q1
 MODEL 0:NPN
 IB 2.504E-06
 IC 5.009E-04
 VBE 7.571E-01
 VCE 3.497E+00
 VBC -2.740E+00
 VS -3.497E+00
 POWER 1.754E-03
 BETAD 2.000E+02
 GM 1.937E-02
 RPI 1.032E+04
 RI 3.000E+02
 RO 2.741E+16
 CPI 5.849E-12
 CMU 1.806E-13
 CBX 0.
 CCS 0.
 BETAAC 2.000E+02
 FT 5.112E+08

**** SMALL-SIGNAL TRANSFER CHARACTERISTICS

V(2)/VI = -3.839E+01
 INPUT RESISTANCE AT VI = 1.562E+04
 OUTPUT RESISTANCE AT V(2) = 3.000E+03

***** AC ANALYSIS

TNOM= 27.000 TEMP= 27.000

FREQ	VDB(2)					
1.000E+05	3.16E+01	-4.000E+01	-2.000E+01	0.	2.000E+01	4.000E+01
1.258E+05	3.16E+01					
1.584E+05	3.16E+01					
1.995E+05	3.16E+01					
2.511E+05	3.16E+01					
3.162E+05	3.16E+01					
3.981E+05	3.15E+01					
5.011E+05	3.15E+01					
6.309E+05	3.14E+01					
7.943E+05	3.13E+01					
1.000E+06	3.11E+01					
1.258E+06	3.08E+01					
1.584E+06	3.04E+01					
1.995E+06	2.99E+01					
2.511E+06	2.90E+01					
3.162E+06	2.80E+01					
3.981E+06	2.67E+01					
5.011E+06	2.52E+01					
6.309E+06	2.36E+01					
7.943E+06	2.19E+01					
1.000E+07	2.01E+01					
1.258E+07	1.82E+01					
1.584E+07	1.62E+01					
1.995E+07	1.43E+01					
2.511E+07	1.23E+01					
3.162E+07	1.03E+01					
3.981E+07	8.39E+00					
5.011E+07	6.39E+00					
6.309E+07	4.38E+00					
7.943E+07	2.37E+00					
1.000E+08	3.56E-01					
1.258E+08	-1.67E+00					
1.584E+08	-3.73E+00					
1.995E+08	-5.82E+00					
2.511E+08	-7.95E+00					
3.162E+08	-1.01E+01					
3.981E+08	-1.24E+01					
5.011E+08	-1.49E+01					
6.309E+08	-1.75E+01					
7.943E+08	-2.03E+01					
1.000E+09	-2.34E+01					

FREQ	VP(2)					
1.000E+05	1.77E+02	5.000E+01	1.000E+02	1.500E+02	2.000E+02	
1.258E+05	1.77E+02					
1.584E+05	1.76E+02					
1.995E+05	1.75E+02					
2.511E+05	1.74E+02					
3.162E+05	1.73E+02					
3.981E+05	1.71E+02					
5.011E+05	1.69E+02					
6.309E+05	1.67E+02					
7.943E+05	1.63E+02					
1.000E+06	1.59E+02					
1.258E+06	1.55E+02					
1.584E+06	1.49E+02					
1.995E+06	1.43E+02					
2.511E+06	1.37E+02					
3.162E+06	1.30E+02					
3.981E+06	1.24E+02					
5.011E+06	1.18E+02					
6.309E+06	1.13E+02					
7.943E+06	1.08E+02					
1.000E+07	1.04E+02					
1.258E+07	1.01E+02					
1.584E+07	9.86E+01					
1.995E+07	9.63E+01					
2.511E+07	9.44E+01					
3.162E+07	9.26E+01					
3.981E+07	9.10E+01					
5.011E+07	8.95E+01					
6.309E+07	8.79E+01					
7.943E+07	8.62E+01					
1.000E+08	8.44E+01					
1.258E+08	8.22E+01					
1.584E+08	7.97E+01					
1.995E+08	7.66E+01					
2.511E+08	7.30E+01					
3.162E+08	6.86E+01					
3.981E+08	6.35E+01					
5.011E+08	5.76E+01					
6.309E+08	5.10E+01					
7.943E+08	4.39E+01					
1.000E+09	3.66E+01					

$$g_m = \sqrt{2k_n' \frac{W}{L} I_D} = \sqrt{2 \times 60 \times 10^{-6} \times \frac{100}{2 \times 2 \times 0.2} \times 500 \times 10^{-6}}$$

$$= 1.9 \times 10^{-3} \text{ A/V}$$

$$A_v = -g_m R_L = -1.9 \times 10^{-3} \times 5 \times 10^3 = -9.5$$

$$C_{gs} = \frac{2}{3} W L_{eff} C_{ox} + W L_d C_{ox}$$

$$= \frac{2}{3} 100 \times 1.6 \times 0.7 + 100 \times 0.2 \times 0.7$$

$$= 89 \text{ fF}$$

$$C_{gd} = W L_d C_{ox} = 100 \times 0.2 \times 0.7 = 14 \text{ fF}$$

(a) Use the Miller effect.

$$|P_1| = \frac{1}{R_s [C_{gs} + C_{gd}(1 - A_v)]}$$

$$= \frac{1}{.10k [89 + 14(1 + 9.5)] \times 10^{-15}}$$

$$= \frac{1}{2.4 \times 10^{-9}} = 4.2 \times 10^8 \text{ rad/s}$$

$$f_{-3dB} = \frac{|P_1|}{2\pi} = 67 \text{ MHz}$$

(b) Do not use the Miller effect to calculate the second pole.

From Eq. (7.26),

$$|P_2| = \frac{1}{|A_v| R_L R_s C_{gd} C_{gs}}$$

$$= \frac{1}{4.2 \times 10^8 \times 5k \times .10k \times 14 \text{ f} \times 89 \text{ f}}$$

$$= 3.8 \times 10^{10} \text{ rad/s}$$

It is equivalent to 6.1 GHz.

```
COMMON SOURCE AMPLIFIER
VDD 1 0 5
VI 2 0 DC 1.216 AC 1
RS 2 3 10K
RL 1 4 5K
M1 4 3 0 0 CMOSN W=100U L=2U
* COX'=0.7FF/UM**2=BOX/TOX => TOX=500 ANGSTROMS
.MODEL CMOSN NMOS LKVEL=1 LAMBDA=0 VTO=0.7 KP=60U LD=0.2U TOX=500E-10
.OPTIONS NOMOD
.AC DEC 10 1MEG 10G
.PLOT AC VM(4)
.WIDTH OUT=80
.OPTIONS SPICE
.END
```

```
***** OPERATING POINT INFORMATION          TNSM= 27.000 TEMP= 27.000
+0:1      = 5.000E+00 0:2      = 1.216E+00 0:3      = 1.216E+00
+0:4      = 2.503E+00
```

```
**** MOSFETS
SUBCIR
ELEMENT 0:M1
MODEL 0:CMOSN
ID 4.992E-04
IBS 0.
IRD -2.504E-14
VGS 1.216E+00
VDS 2.503E+00
VBS 0.
VTH 7.000E-01
VDSAT 5.160E-01
BETA 3.750E-03
GAM KFF 0.
GM 1.935E-03
GDS 0.
GMS 0.
COTOT 1.418E-14
COTOT 1.050E-13
CSTOT 8.748E-14
CBTOT 3.349E-15
CGS 8.748E-14
CGD 1.418E-14
```

```
***** AC ANALYSIS          TNSM= 27.000 TEMP= 27.000
```

FREQ	VM(4)	1.000E-02	1.000E-01	1.000E+00	9.999E+00	9.999E+01
1.000E+06	9.67E+00					
1.258E+06	9.67E+00	+	+	+	+	A
1.584E+06	9.67E+00	+	+	+	+	A
1.995E+06	9.67E+00	+	+	+	+	A
2.511E+06	9.66E+00	+	+	+	+	A
3.162E+06	9.66E+00	+	+	+	+	A
3.981E+06	9.65E+00	+	+	+	+	A
5.011E+06	9.64E+00	+	+	+	+	A
6.309E+06	9.62E+00	+	+	+	+	A
7.943E+06	9.60E+00	+	+	+	+	A
1.000E+07	9.56E+00					
1.258E+07	9.49E+00	+	+	+	+	A
1.584E+07	9.39E+00	+	+	+	+	A
1.995E+07	9.24E+00	+	+	+	+	A
2.511E+07	9.01E+00	+	+	+	+	A
3.162E+07	8.68E+00	+	+	+	+	A
3.981E+07	8.23E+00	+	+	+	+	A
5.011E+07	7.64E+00	+	+	+	+	A
6.309E+07	6.91E+00	+	+	+	+	A
7.943E+07	6.09E+00	+	+	+	+	A
1.000E+08	5.24E+00					
1.258E+08	4.41E+00	+	+	+	+	A
1.584E+08	3.64E+00	+	+	+	+	A
1.995E+08	2.97E+00	+	+	+	+	A
2.511E+08	2.40E+00	+	+	+	+	A
3.162E+08	1.93E+00	+	+	+	+	A
3.981E+08	1.54E+00	+	+	+	+	A
5.011E+08	1.23E+00	+	+	+	+	A
6.309E+08	9.79E-01	+	+	+	+	A
7.943E+08	7.77E-01	+	+	+	+	A
1.000E+09	6.15E-01					
1.258E+09	4.86E-01	+	+	+	+	A
1.584E+09	3.82E-01	+	+	+	+	A
1.995E+09	2.98E-01	+	+	+	+	A
2.511E+09	2.31E-01	+	+	+	+	A
3.162E+09	1.77E-01	+	+	+	+	A
3.981E+09	1.33E-01	+	+	+	+	A
5.011E+09	9.87E-02	+	+	+	+	A
6.309E+09	7.16E-02	+	+	+	+	A
7.943E+09	5.09E-02	+	+	+	+	A
1.000E+10	3.58E-02					

7.8

$$\frac{v_o}{v_i} = \frac{g_m R_E + \frac{R_E}{r_\pi}}{1 + g_m R_E + \frac{R_b + R_E}{r_\pi}} \frac{1 - \frac{s}{z_1}}{1 - \frac{s}{p_1}}$$

$$= \frac{\frac{0.3 \times 4000 + \frac{4000}{50} \cdot \frac{0.3}{26}}{1 + \frac{0.3 \times 4000 + \frac{4450}{50} \cdot \frac{0.3}{26}}}{1 - \frac{j\omega}{z_1}} \frac{1 - \frac{j\omega}{z_1}}{1 - \frac{j\omega}{p_1}}$$

$$= 0.977 \frac{1 - j \frac{\omega}{z_1}}{1 - j \frac{\omega}{p_1}}$$

$$z_1 = -\frac{g_m}{C_\pi} = -\omega_T = -2\pi \times 4 \times 10^6$$

$$= -25.1 \times 10^6 \text{ rad/sec}$$

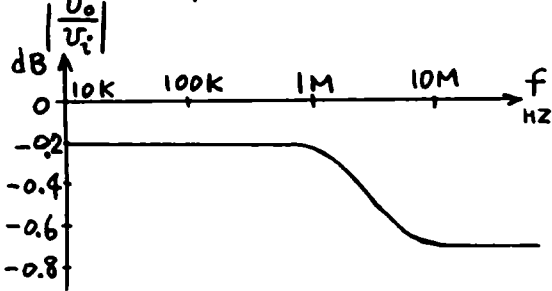
$$p_1 = -\frac{1}{C_\pi R_1}$$

$$R_1 = r_\pi \parallel \frac{R_b + R_E}{1 + g_m R_E} = \frac{50 \times 26}{0.3} \parallel \frac{450 + 4000}{1 + \frac{0.3 \times 4000}{26}}$$

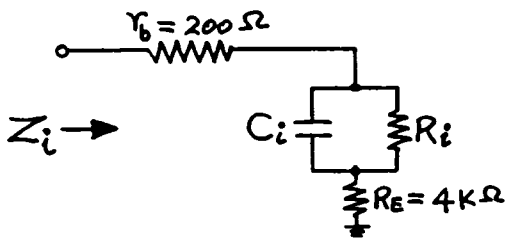
$$= 4333 \parallel 94.4 = 92.4 \Omega$$

$$C_\pi = \frac{g_m}{\omega_T} = \frac{0.3}{26} \frac{1}{2\pi \times 4 \times 10^6} = 459 \text{ pF}$$

$$\therefore p_1 = -\frac{10^{12}}{459 \times 92.4} = -23.6 \times 10^6 \text{ rad/sec}$$



7.9

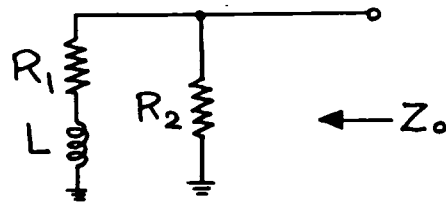


$$C_i = \frac{C_\pi}{1 + g_m R_E} = \frac{459}{1 + \frac{0.3 \times 4000}{26}} = 9.73 \text{ pF}$$

$$R_i = (1 + g_m R_E) r_\pi = \left(1 + \frac{0.3 \times 4000}{26}\right) \times \frac{50 \times 26}{0.3}$$

$$= 204 \text{ k}\Omega$$

$$Z_i = 4.2 \text{ k}\Omega + 204 \text{ k}\Omega \parallel \frac{1}{j\omega C_i}$$

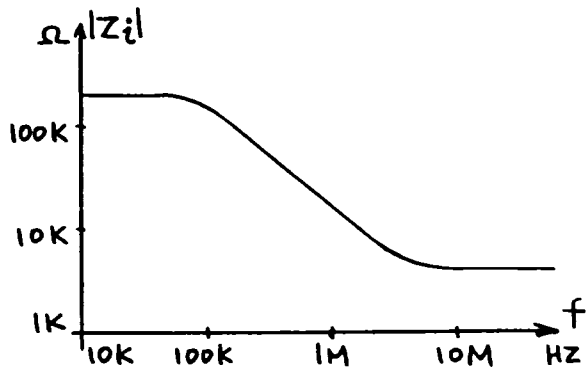
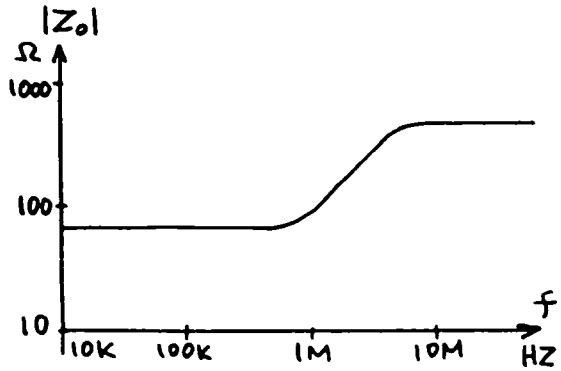


$$R_1 = \frac{1}{g_m} + \frac{R_b}{\beta_0} = \frac{26}{0.3} + \frac{450}{50} = 95.7 \Omega$$

$$R_2 = R_b = 450 \Omega$$

$$L = C_\pi r_\pi \frac{R_b}{\beta_0} = 459 \times \frac{50 \times 26}{0.3} \times \frac{450}{50} \times 10^{-12}$$

$$= 17.9 \mu\text{H}$$



```

PNP EMITTER FOLLOWER, RESISTIVE LOAD
* DC VO=0V, 300UA*4K=1.2V=VCC
VCC 1 0 1.2V
VEE 2 0 -1.2V
RE 1 5 4K
Q1 2 4 5 PNP
RS 3 4 250
RLOAD 5 0 1K
VBIAS 3 6 -0.745V AC
VPULSE 6 0 PULSE 0V 1MV 1NS 0NS 0NS 100NS
.TRAN 0.25MS 10NS
.PLOT TRAN V(5)
.MODEL PNP PNP IS=1E-16A BF=50
+ RB=200 CJE=0 CJC=0 CJS=0 TF=39.8NS
.OPTIONS NOPAGE NOMOD
.WIDTH OUT=80
.OPTIONS SPICE
.OP
.END

```

```

***** OPERATING POINT INFORMATION          TNOM= 27.000 TEMP= 27.000

+0:1      = 1.200E+00 0:2      = -1.200E+00 0:3      = -7.450E-01
+0:4      = -7.435E-01 0:5      = 1.819E-04 0:6      = 0.

```

**** BIPOLAR JUNCTION TRANSISTORS

```

ELEMENT 0:Q1
MODEL 0:PNP
IB -5.878E-06
IC -2.939E-04
VBE -7.437E-01
VCE -1.200E+00
VBC 4.565E-01
VS 7.424E-01
POWER 3.571E-04
BETAD 5.000E+01
GM 1.137E-02
RPI 4.400E+03
RX 2.000E+02
RO 4.576E+15
CPI 4.522E-10
CMU 0.
CBX 0.
CCS 0.
BETAAC 5.000E+01
FT 3.998E+06

```

***** TRANSIENT ANALYSIS TNOM= 27.000 TEMP= 27.000

TIME	V(5)
0.	1.82E-04
2.500E-10	1.82E-04
5.000E-10	1.82E-04
7.500E-10	1.82E-04
1.000E-09	1.82E-04
1.250E-09	8.23E-04
1.500E-09	8.24E-04
1.750E-09	8.25E-04
2.000E-09	9.76E-04
2.250E-09	8.27E-04
2.500E-09	8.28E-04
2.750E-09	8.29E-04
3.000E-09	8.31E-04
3.250E-09	8.32E-04
3.500E-09	8.33E-04
3.750E-09	8.34E-04
4.000E-09	8.35E-04
4.250E-09	8.36E-04
4.500E-09	8.37E-04
4.750E-09	8.38E-04
5.000E-09	8.39E-04
5.250E-09	8.40E-04
5.500E-09	8.42E-04
5.750E-09	8.43E-04
6.000E-09	8.44E-04
6.250E-09	8.45E-04
6.500E-09	8.46E-04
6.750E-09	8.47E-04
7.000E-09	8.48E-04
7.250E-09	8.49E-04
7.500E-09	8.50E-04
7.750E-09	8.51E-04

**** PNP EMITTER FOLLOWER, CAPACITIVE LOAD

```

VCC 1 0 1.2V
VEE 2 0 -1.2V
IER 1 5 300UA
Q1 2 4 5 PNP
RS 3 4 250
CLOAD 5 0 400PF
VBIAS 3 6 -0.745V AC
VPULSE 6 0 PULSE 0V 1MV 1NS 0NS 0NS 1300NS
.TRAN 20NS 800NS

```

```

.PLOT TRAN V(5)
.MODEL PNP PNP IS=1E-16A BF=50
+ RB=200 CJE=0 CJC=0 CJS=0 TF=39.8NS
.OPTIONS NOPAGE NOMOD
.WIDTH OUT=80
.OPTIONS SPICE
.OP
.END

```

**** BIPOLAR JUNCTION TRANSISTORS

```

ELEMENT 0:Q1
MODEL 0:PNP
IB -5.882E-06
IC -2.941E-04
VBE -7.437E-01
VCE -1.200E+00
VBC 4.565E-01
VS 7.424E-01
POWER 3.574E-04
BETAD 5.000E+01
GM 1.137E-02
RPI 4.396E+03
RX 2.000E+02
RO 4.576E+15
CPI 4.526E-10
CMU 0.
CBX 0.
CCS 0.
BETAAC 5.000E+01
FT 3.998E+06

```

***** TRANSIENT ANALYSIS TNOM= 27.000 TEMP= 27.000

TIME	V(5)	5.000E-04	1.000E-03	1.500E-03	2.000E-03
0.	2.03E-04				
2.000E-08	2.59E-04	A			
4.000E-08	3.94E-04	A			
6.000E-08	5.42E-04	A			
8.000E-08	6.95E-04	A			
1.000E-07	8.44E-04	A			
1.200E-07	9.81E-04	A			
1.400E-07	1.10E-03	A			
1.600E-07	1.21E-03	A			
1.800E-07	1.29E-03	A			
2.000E-07	1.35E-03	A			
2.200E-07	1.39E-03	A			
2.400E-07	1.42E-03	A			
2.600E-07	1.43E-03	A			
2.800E-07	1.42E-03	A			
3.000E-07	1.41E-03	A			
3.200E-07	1.39E-03	A			
3.400E-07	1.36E-03	A			
3.600E-07	1.33E-03	A			
3.800E-07	1.30E-03	A			
4.000E-07	1.27E-03	A			
4.200E-07	1.24E-03	A			
4.400E-07	1.22E-03	A			
4.600E-07	1.20E-03	A			
4.800E-07	1.18E-03	A			
5.000E-07	1.17E-03	A			
5.200E-07	1.16E-03	A			
5.400E-07	1.16E-03	A			
5.600E-07	1.16E-03	A			
5.800E-07	1.16E-03	A			
6.000E-07	1.16E-03	A			
6.200E-07	1.17E-03	A			
6.400E-07	1.17E-03	A			
6.600E-07	1.19E-03	A			
6.800E-07	1.19E-03	A			
7.000E-07	1.19E-03	A			
7.200E-07	1.20E-03	A			
7.400E-07	1.20E-03	A			
7.600E-07	1.20E-03	A			
7.800E-07	1.21E-03	A			
8.000E-07	1.21E-03	A			

***** CAPACITIVE LOAD RESULTS IN SOME PEAKING [V(5) JUMPS BY > 1MV]