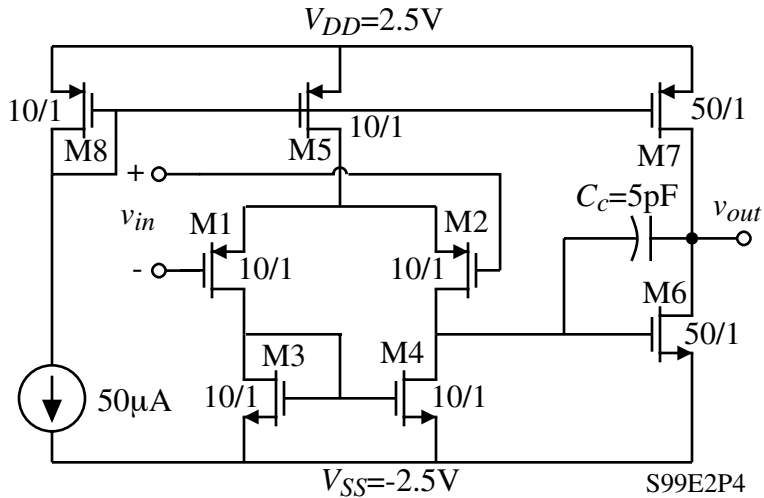


## Homework Assignment No. 6 - Solutions

### Problem 1 - (10 points)

For the CMOS op amp shown, find the following quantities.

- 1.) Slew rate (V/sec.)
- 2.) Positive and negative output voltage limits (all transistors remain in saturation)
- 3.) Positive and negative input common voltage limits (all transistors remain in saturation and use nominal parameter values)
- 4.) Small signal voltage gain
- 5.) Unity-gainbandwidth (MHz) and 6.) Power dissipation (mW).



### Solution

$$1.) \quad SR = \frac{I_5}{C_c} = \frac{50\mu\text{A}}{5\text{pF}} = 10^7 \text{V/second} \quad \Rightarrow \quad \boxed{SR = 10^7 \text{V/sec}}$$

$$2.) \quad V_{SD7} = \sqrt{\frac{2I_7}{K_P(W/L)}} = \sqrt{\frac{500\mu\text{A}}{50 \cdot 50}} = 0.447\text{V} \quad \text{and} \quad V_{DS6} = \sqrt{\frac{500\mu\text{A}}{110 \cdot 50}} = 0.3015\text{V}$$

$$\therefore \quad \boxed{V_{out}(\text{max}) = 2.5 - 0.447 = 2.053\text{V}} \quad \&$$

$$\boxed{V_{out}(\text{min}) = -2.5\text{V} + 0.3015\text{V} = -2.198\text{V}}$$

$$3.) \quad ICM(\text{min}) = -2.5\text{V} + V_{GS3} - |V_{TP}| = -2.5\text{V} + \sqrt{\frac{2 \cdot 25}{110 \cdot 10}} + 0.7\text{V} - 0.7\text{V}$$

$$\therefore \quad ICM(\text{min}) = -2.5 + 0.213 = -2.287\text{V} \quad \Rightarrow \quad \boxed{ICM(\text{min}) = -2.287\text{V}}$$

$$ICM(\text{max}) = ? \quad V_{SD5}(\text{sat}) = \sqrt{\frac{2 \cdot 50}{50 \cdot 10}} = 0.4472\text{V} \quad \text{and} \quad V_{SG1} = \sqrt{\frac{2 \cdot 25}{50 \cdot 10}} + 0.7 = 1.016\text{V}$$

$$\therefore \quad ICM(\text{max}) = 2.5 - V_{SD5}(\text{sat}) - V_{SG1} = 2.5 - 0.4472 - 1.016 = 1.0366\text{V}$$

$$\boxed{ICM(\text{max}) = 1.0366\text{V}}$$

$$4.) \quad A_v = \frac{g_{m1}g_{m6}}{(g_{sd2} + g_{ds4})(g_{ds6} + g_{sd7})} \quad g_{m1} = \sqrt{\frac{2K_P W_1 I_1}{L_1}} = \sqrt{2 \cdot 50 \cdot 10 \cdot 25} = 158\mu\text{S}$$

$$g_{m6} = \sqrt{\frac{2K_P W_6 I_6}{L_6}} = \sqrt{2 \cdot 110 \cdot 50 \cdot 250} = 1658\mu\text{S} \quad G_I = 0.09 \cdot 250\mu\text{A} = 2.25\mu\text{S}$$

$$\text{and} \quad G_{II} = 0.09 \cdot 250\mu\text{A} = 22.5\mu\text{S}$$

$$\therefore \quad A_v = \frac{158 \cdot 1658}{2.25 \cdot 22.5} = 3,489\text{V/V} \quad \Rightarrow \quad \boxed{A_v = 5,176\text{V/V}}$$

$$5.) \quad GB = \frac{g_{m1}}{C_c} = \frac{158\mu\text{S}}{5\text{pF}} = 31.6\text{Mrads/sec} \quad \Rightarrow \quad \boxed{GB = 5.03\text{MHz}}$$

$$6.) \quad P_{diss} = 5 \times 350\mu\text{A} = 1.75\text{mW} \quad \Rightarrow \quad \boxed{P_{diss} = 1.75\text{mW}}$$

Problem 2 - (10 points)

Bias current calculation:

$$V_{T8} + V_{ON8} + I_8 \cdot R_S = V_{dd} - V_{ss} \quad \text{or,} \quad V_{T8} + \sqrt{\frac{2 \cdot I_8}{3 \cdot K'_p}} = 5 - I_8 \cdot R_S \quad (1)$$

Solving for  $I_8$  quadratically would give,  $I_8 = \underline{36\mu A}$ ,  $I_5 = \underline{36\mu A}$ , and  $I_7 = \underline{60\mu A}$ Using the formula,  $g_m = \sqrt{2 \cdot K' \frac{W}{L} I}$  and  $g_{ds} = \lambda I$  we get,

$$g_{m2} = 60\mu S, \quad g_{ds2} = 0.9\mu S, \quad g_{ds4} = 0.72\mu S \quad (2)$$

$$g_{m6} = 363\mu S, \quad g_{ds6} = 3\mu S, \quad g_{ds7} = 2.4\mu S \quad (3)$$

Small-signal open-loop gain:

The small-signal voltage gain can be expressed as,

$$A_{v1} = \frac{-g_{m2}}{(g_{ds2} + g_{ds4})} = -37 \quad \text{and} \quad A_{v2} = \frac{-g_{m6}}{(g_{ds6} + g_{ds7})} = -67$$

Thus, total open-loop gain is,

$$A_v = A_{v1} \cdot A_{v2} = \underline{2489V/V} \quad (3)$$

Output resistance:

$$R_{out} = \frac{1}{(g_{ds6} + g_{ds7})} = 185K\Omega \quad (5)$$

Power dissipation:

$$P_{diss} = 5(36 + 36 + 60)\mu W = 660\mu W \quad (6)$$

ICMR:

$$V_{in,max} = 2.5 - V_{T1} - V_{ON1} - V_{ON5} = 0.51V \quad (7)$$

$$V_{in,min} = -2.5 - V_{T1} + V_{T3} + V_{ON3} = -2.21V \quad (8)$$

Output voltage swing:

$$V_{0,max} = 2.5 - V_{ON7} = 1.81V \quad (9)$$

Slew Rate:

Slew rate under no load condition can be given as,

$$SR = \frac{I_5}{C_c} = 6V / \mu s$$

In presence of a load capacitor of 20 pF, slew rate would be,

$$SR = \min\left[\frac{I_5}{C_c}, \frac{I_7}{C_L}\right]$$

Problem 6.3-7 - Continued

CMRR:

Under perfectly balanced condition where  $I_1 = I_2$ , if a small signal common-mode variation occurs at the two input terminals, the small signal currents  $i_1 = i_2 = i_3 = i_4$  and the differential output current at node (7) is zero. So, ideally, common-mode gain would be zero and the value for CMRR would be infinity.

GBW:

Let us design M9 and M10 first. Both these transistors would operate in triode region and will carry zero dc current. Thus,  $V_{ds9} = V_{ds10} \cong 0$ . The equation of drain current in triode region is given as,

$$I_D \cong K' \frac{W}{L} (V_{GS} - V_T) V_{DS}.$$

The on resistance of the MOS transistor in triode region of operation would be,

$$R_{ON} = K' \frac{W}{L} (V_{GS} - V_T).$$

It is intended to make the effective resistance of M9 and M10 equal to  $\frac{1}{g_{m6}}$ .

$$\text{So, } K'_9 \left( \frac{W_9}{L_9} \right) (V_{GS9} - V_{T9}) + K'_{10} \left( \frac{W_{10}}{L_{10}} \right) (V_{GS10} - V_{T10}) = g_{m6} \quad (11)$$

$$V_{D4} = V_{D3} = -2.5 + V_{T3} + V_{ON3} = -1.51V$$

Thus,

$$V_{GS9} \cong 4V \quad \text{and} \quad V_{GS10} \cong -1V.$$

Putting the appropriate values in (11), we can solve for the aspect ratios of M9 and M10. One of the solutions could be,

$$K'_9 \left( \frac{W_9}{L_9} \right) = \frac{1}{1} \quad \text{and} \quad K'_{10} \left( \frac{W_{10}}{L_{10}} \right) = \text{very small} \quad (12)$$

The dominant pole could be calculated as,

$$p_1 = \frac{-(g_{ds4} + g_{ds2})}{2\pi \cdot A_{V1} \cdot C_C} = -1.16 \text{ KHz.}$$

And the load pole would be,

$$p_2 = \frac{-g_{m6}}{2\pi \cdot C_L} = -2.8 \text{ MHz.} \quad \text{for a 20 pF load.}$$

It can be noted that in this problem, the product of the open-loop gain and the dominant pole is approximately equal to the load pole. Thus, the gain bandwidth is approximately equal to 2.8 MHz and the phase margin would be close to 45 degrees.

Problem 6.3-7 - Continued

PSRR:

If a small ripple  $v_s$  is applied at the  $V_{dd}$  terminal, then the gain of this ripple from this terminal to the output can be expressed as,

$$\frac{v_o}{v_s} = \frac{\left(1 - \frac{R_S}{R_S + (1/g_{m8})}\right) g_{m7}}{g_{ds6} + g_{ds7}} = 2.8V/V$$

Thus, PSRR due to variations in  $V_{dd}$  would be,  $A_V \mu.8 = 2489 / 2.8 = 889$  .

SPICE file:

```
.model nmos nmos vto=0.7 lambda=0.04 kp=110u
.model pmos pmos vto=-0.8 lambda=0.05 kp=50u

vdd 1 0 dc 2.5 ac 0
vss 10 0 dc -2.5 ac 0
vinp 5 0 dc 0 ac 1
*vinn 4 0 dc 0 ac 0

m8 2 2 1 1 pmos w=3u l=1u
rs 2 10 100k
m5 3 2 1 1 pmos w=3u l=1u
m1 6 8 3 3 pmos w=2u l=1u
m2 7 5 3 3 pmos w=2u l=1u
m3 6 6 10 10 nmos w=4u l=1u
m4 7 6 10 10 nmos w=4u l=1u
m7 8 2 1 1 pmos w=5u l=1u
m6 8 7 10 10 nmos w=10u l=1u
cc 7 9 6p
cl 8 0 20p
m9 8 1 9 9 nmos w=1u l=1u
m10 8 10 9 9 pmos w=1u l=100u

.op
.ac dec 10 1 100meg
.option post
.end

Operating points:

**** mosfets

subckt
element 0:m8      0:m5      0:m1      0:m2      0:m3      0:m4
model      0:pmos      0:pmos      0:pmos      0:pmos      0:nmos      0:nmos
region      Cutoff      Cutoff      Cutoff      Cutoff      Saturati    Saturati
id         -35.3708u    -34.8506u    -17.4107u    -17.4399u    17.4107u    17.4399u
ibs         0.          0.          0.          0.          0.          0.
ibd         14.6292f     11.4726f     28.7676f     28.3314f     -9.7598f    -10.1959f
```

Problem 6.3-7 - Continued

vgs	-1.4629	-1.4629	-1.3517	-1.3527	975.9818m	975.9818m
vds	-1.4629	-1.1473	-2.8768	-2.8331	975.9818m	1.0196
vbs	0.	0.	0.	0.	0.	0.
vth	-800.0000m	-800.0000m	-800.0000m	-800.0000m	700.0000m	700.0000m
vdsat	-662.9217m	-662.9217m	-551.7476m	-552.7377m	275.9818m	275.9818m
beta	160.9719u	158.6045u	114.3838u	114.1657u	457.1773u	457.9449u
gam eff	527.6252m	527.6252m	527.6252m	527.6252m	527.6252m	527.6252m
gm	106.7118u	105.1423u	63.1110u	63.1037u	126.1726u	126.3844u
gds	1.6480u	1.6480u	761.0636n	763.7975n	670.2604n	670.2604n
gmb	36.9704u	36.4266u	21.8648u	21.8623u	43.7126u	43.7860u
cdtot	2.021e-18	1.585e-18	2.649e-18	2.609e-18	1.797e-18	1.878e-18
cgtot	7.005e-16	7.000e-16	4.693e-16	4.692e-16	9.467e-16	9.467e-16
cstot	6.906e-16	6.906e-16	4.604e-16	4.604e-16	9.208e-16	9.208e-16
cbtot	7.806e-18	7.806e-18	6.216e-18	6.205e-18	2.402e-17	2.402e-17
cgs	6.906e-16	6.906e-16	4.604e-16	4.604e-16	9.208e-16	9.208e-16
cgd	2.021e-18	1.585e-18	2.649e-18	2.609e-18	1.797e-18	1.878e-18

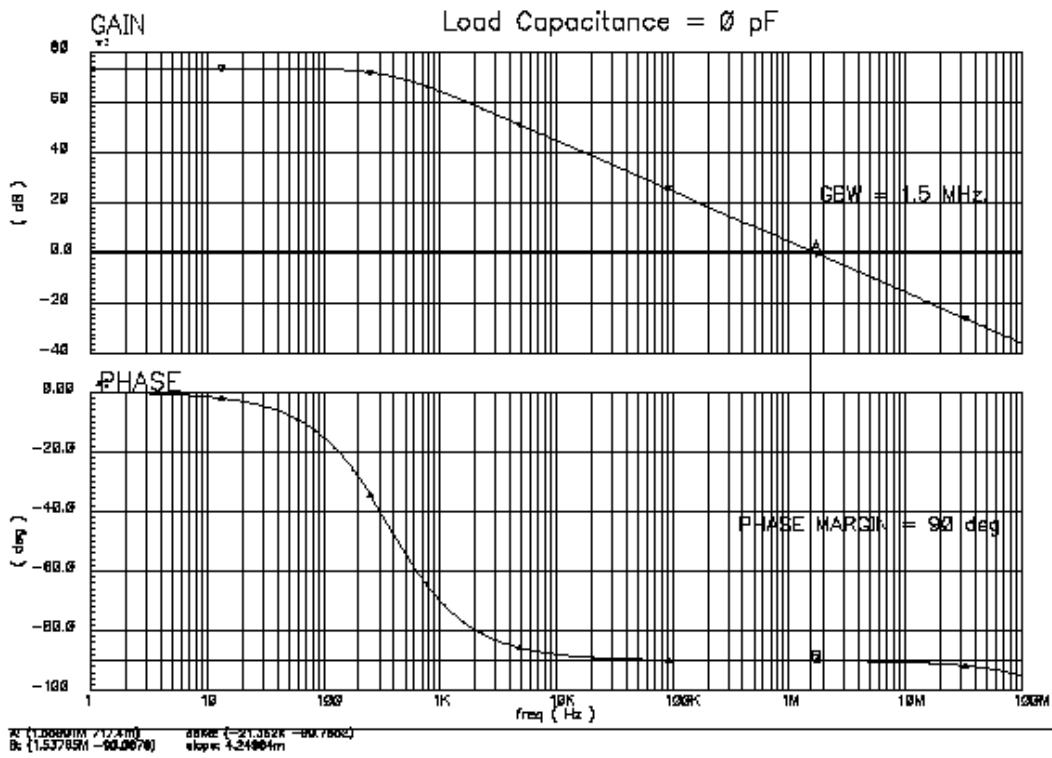
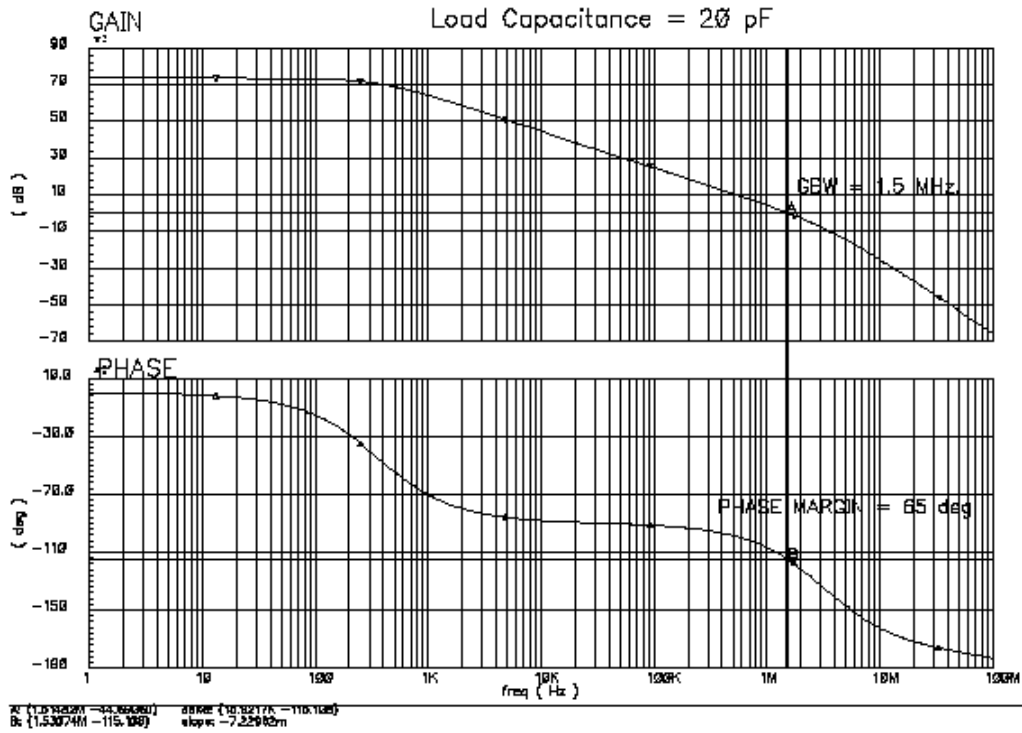
subckt

element	0:m7	0:m6	0:m9	0:m10
model	0:pmos	0:nmos	0:nmos	0:pmos
region	Cutoff	Saturati	Linear	Cutoff
id	-61.7971u	61.7971u	0.	0.
ibs	0.	0.	0.	0.
ibd	24.9901f	-25.0099f	0.	0.
vgs	-1.4629	1.0196	2.4990	-2.5010
vds	-2.4990	2.5010	0.	0.
vbs	0.	0.	0.	0.
vth	-800.0000m	700.0000m	700.0000m	-800.0000m
vdsat	-662.9217m	319.5939m	0.	0.
beta	281.2376u	1.2100m	110.0000u	500.0000n
gam eff	527.6252m	527.6252m	527.6252m	527.6252m
gm	186.4385u	386.7225u	0.	0.
gds	2.7467u	2.2471u	197.8911u	850.4951n
gmb	64.5917u	133.9802u	0.	0.
cdtot	5.753e-18	1.152e-17	1.727e-16	17.2658f
cgtot	1.1698f	2.3660f	3.463e-16	34.6349f
cstot	1.1511f	2.3021f	1.727e-16	17.2658f
cbtot	1.301e-17	5.233e-17	9.769e-19	1.033e-16
cgs	1.1511f	2.3021f	1.727e-16	17.2658f
cgd	5.753e-18	1.152e-17	1.727e-16	17.2658f

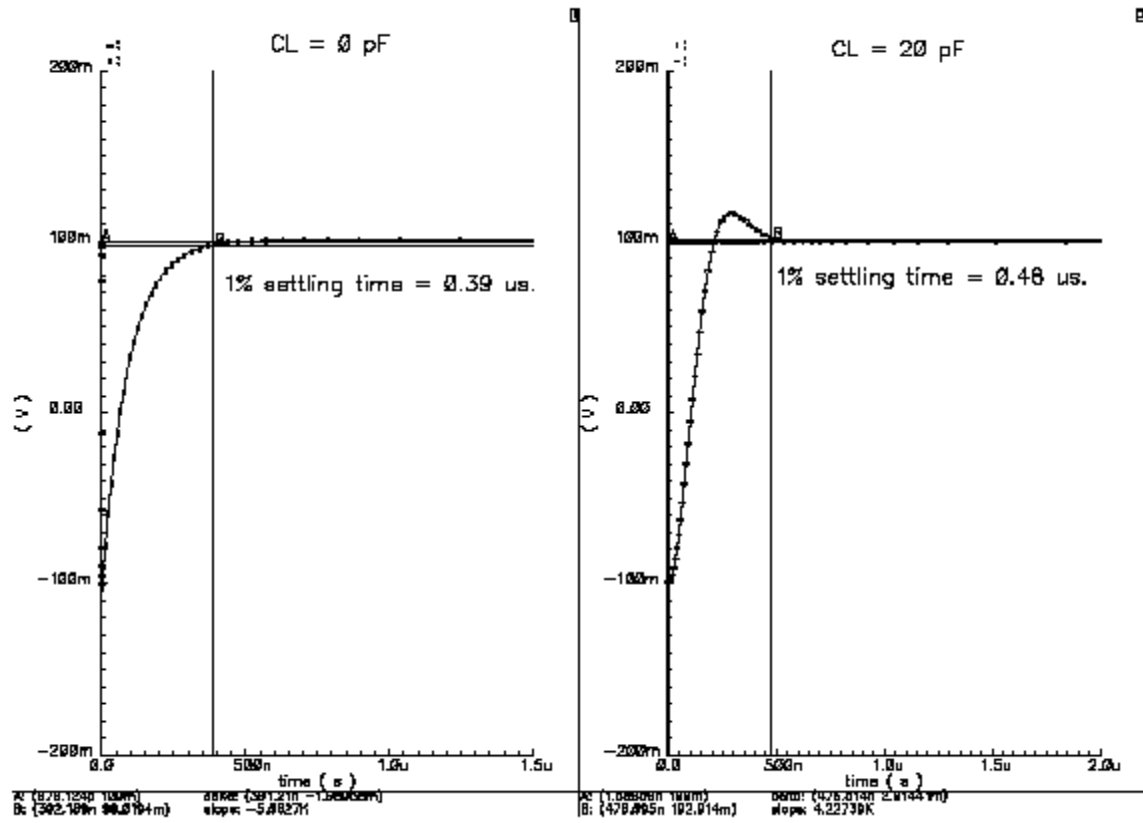
Results from SPICE simulation:

- i. Unloaded output (load capacitor = 0)
  - GBW = 1.5 MHz., Phase Margin = 90 deg, 1% settling time = 0.39 us.
- ii. Loaded output (load capacitor = 20 pF)
  - GBW = 1.5 MHz., Phase Margin = 65 deg, 1% settling time = 0.48 us.

Problem 6.3-7 - Continued



Problem 6.3-7 - Continued



**Problem 3 - (10 points)**

Small signal differential voltage gain:

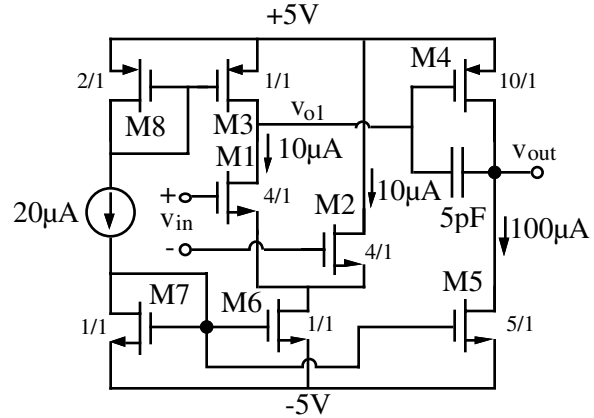
By intuitive analysis methods,

$$\frac{v_{o1}}{v_{in}} = \frac{-0.5g_{m1}}{g_{ds1} + g_{ds3}}$$

and

$$\frac{v_{out}}{v_{o1}} = \frac{-g_{m4}}{g_{ds4} + g_{ds5}}$$

$$\therefore \frac{v_{out}}{v_{in}} = \frac{0.5g_{m1}g_{m4}}{(g_{ds1}+g_{ds3})(g_{ds4}+g_{ds5})}$$



$$g_{m1} = \sqrt{\frac{2K_N W_1 I_{D1}}{L_1}} = \sqrt{24 \cdot 2.4 \cdot 10} \times 10^{-6} = 43.82 \mu\text{S}$$

$$g_{ds1} = \lambda_N I_{D1} = 0.01 \cdot 10 \mu\text{A} = 0.1 \mu\text{S}, \quad g_{ds3} = \lambda_P I_{D3} = 0.02 \cdot 10 \mu\text{A} = 0.2 \mu\text{S}$$

$$g_{m4} = \sqrt{\frac{2K_P W_4 I_{D4}}{L_4}} = \sqrt{2 \cdot 8 \cdot 10 \cdot 100} \times 10^{-6} = 126.5 \mu\text{S}$$

$$g_{ds4} = \lambda_P I_{D4} = 0.02 \cdot 100 \mu\text{A} = 2 \mu\text{S}, \quad g_{ds5} = \lambda_N I_{D5} = 0.01 \cdot 100 \mu\text{A} = 1 \mu\text{S}$$

$$\therefore \frac{v_{out}}{v_{in}} = \frac{0.5 \cdot 43.82 \cdot 126.5}{(0.1 + 0.2)(1 + 2)} = 3,079 \text{ V/V}$$

Output resistance:

$$R_{out} = \frac{1}{g_{ds4} + g_{ds5}} = \frac{10^6}{1 + 2} = 333 \text{ k}\Omega$$

Dominant pole,  $p_1$ :

$$|p_1| = \frac{1}{R_1 C_1} \quad \text{where } R_1 = \frac{1}{g_{ds1} + g_{ds3}} = \frac{10^6}{0.1 + 0.2} = 3.33 \text{ M}\Omega$$

and

$$C_1 = C_c(1 + |A_{v2}|) = 5 \text{ pF} \left( 1 + \frac{g_{m4}}{g_{ds4} + g_{ds5}} \right) = 5 \left( 1 + \frac{126.5}{3} \right) = 215.8 \text{ pF}$$

$$\therefore |p_1| = \frac{10^6}{3.33 \cdot 215.8} = 1,391 \text{ rads/sec} \rightarrow |p_1| = 1,391 \text{ rads/sec} = 221 \text{ Hz}$$

$$\text{GB} = \frac{0.5 \cdot g_{m1}}{C_c} = \frac{0.5 \cdot 43.82 \times 10^{-6}}{5 \times 10^{-12}} = 4.382 \text{ Mrads/sec}$$

$$\text{GB} = 4.382 \text{ Mrads/sec} = 0.697 \text{ MHz}$$

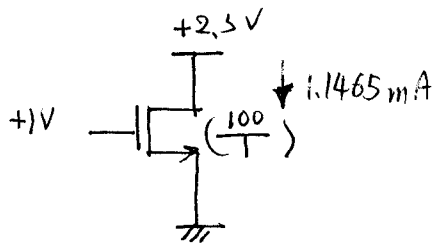
$$\text{SR} = \frac{I_{D6}}{C_c} = \frac{10 \mu\text{A}}{5 \text{ pF}} = 2 \text{ V}/\mu\text{s}$$

$$P_{diss} = 10 \text{ V}(140 \mu\text{A}) = 1.4 \text{ mW}$$



Problem 4 - Design Problem 2 (50 points)

## NMOS Characterization



$$V_{th} = \underline{\underline{0.662 \text{ V}}}$$

$$g_{ds} = \lambda_n I_D \Rightarrow 29.8824 \mu = \lambda_n \times 1.1465 \text{ m}$$

$$\Rightarrow \underline{\underline{\lambda_n = 0.026}}$$

$$g_m^2 = 2 K_n' \frac{W}{L} I_D \Rightarrow [5.8228 \times 10^{-3}]^2 = 2 K_n' \times 100 \times 1.1465 \times 10^{-3}$$

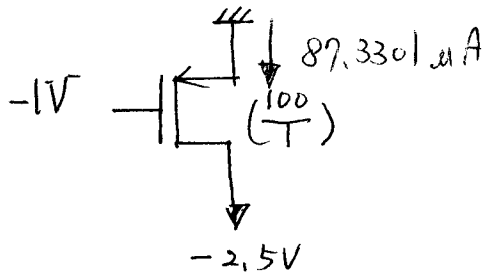
$$\Rightarrow \underline{\underline{K_n' = 147.86 \mu\text{A}/\text{V}^2}}$$

$$\text{Therefore, } \left\{ \begin{array}{l} V_{th} = 0.662 \text{ V} \\ K_n' = 147.86 \mu\text{A}/\text{V}^2 \\ \lambda_n = 0.026 \end{array} \right\}$$

forms the foundation to do

the initial design by hand calculation.

## PMOS Characteristics



$$\underline{V_{th} = -0.864 V} \#$$

$$g_{ds} = \lambda_p I_D \Rightarrow 9.1481 \mu = \lambda_p \times 87.3301 \mu A$$

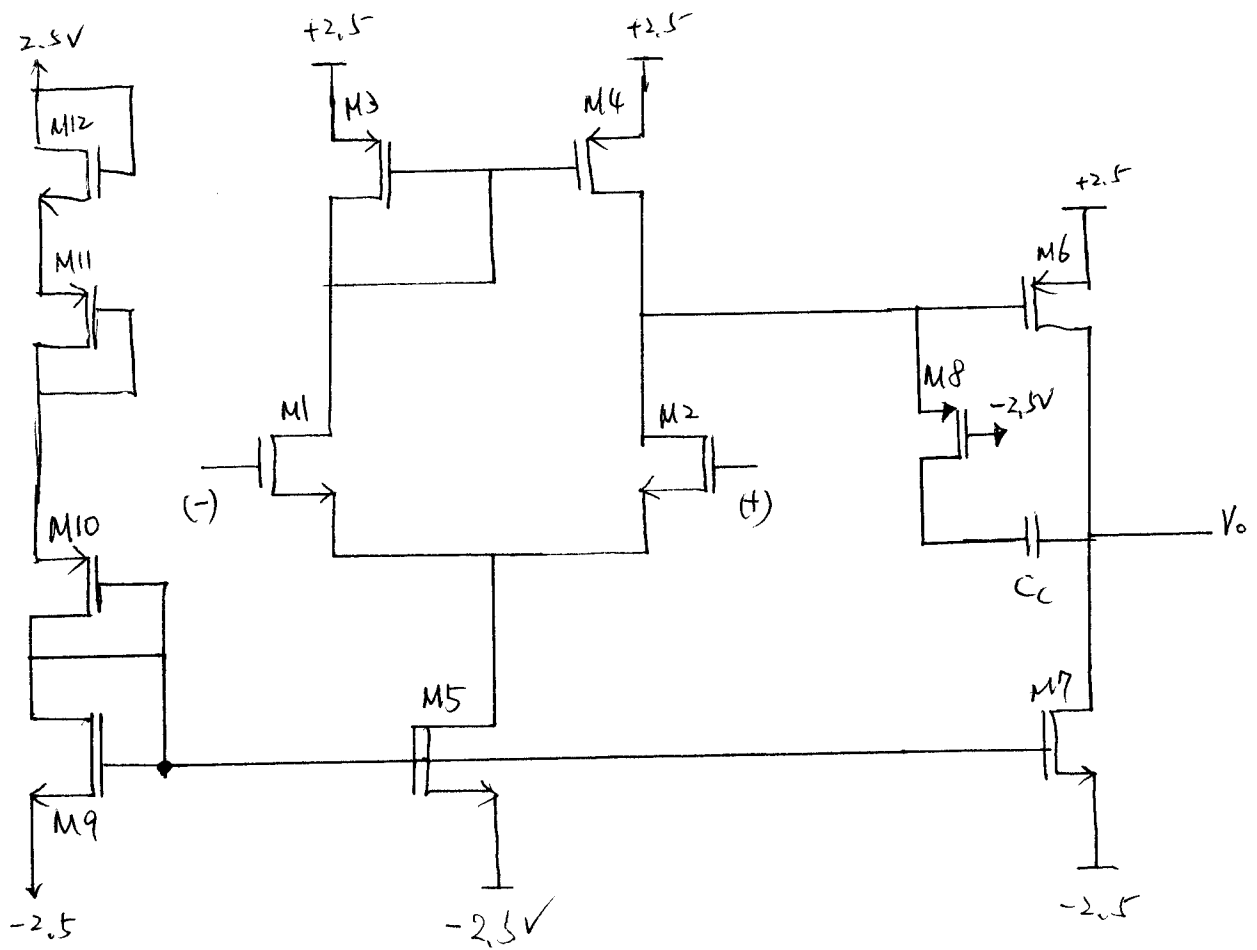
$$\Rightarrow \underline{\lambda_p = 0.105} \#$$

$$g_m^2 = 2k_p' \frac{W}{L} I_D \Rightarrow [1.0091 \times 10^{-3}]^2 = 2k_p' \times 100 \times 87.3301 \times 10^{-6}$$

$$\Rightarrow \underline{k_p' = 58.3 \mu A/V^2} \#$$

Therefore  $\left\{ \begin{array}{l} V_{th} = -0.864 V \\ k_p' = 58.3 \mu A/V^2 \\ \lambda_p = 0.105 \end{array} \right\}$  forms the basis to do the initial design by hand calculation.

# Structure



- Explanation:
- (1) M10, M9. set up the bias voltage at gate of M9. then M9, M5, M7 are current mirrors to set up the bias currents for differential pair and M7 is a constant current sink load with respect to M6.
  - (2) M1, M2 differential pair with current mirror load consisting of M3 and M4. this is the first stage of the amplifier and the gain is  $g_{m1} R_{E1}$ .  $g_{m1}$  is  $g_{m1} = g_{m12} = g_{m10}$  and  $R_{E1} = Y_{as2} \parallel R_{ds4}$ .
  - (3) M6 is a common source amplifier with a constant sink load to get a high gain hopefully.
  - (4) M8 acts as a resistor AC wise to create nulling zeros with Cc.

(1) Power consumption consideration =

$$[2.5 - (-2.5)] I_{\text{total}} \leq 1 \text{ mW}$$

$$\Rightarrow \underline{I_{\text{total}} \leq 200 \mu\text{A}}$$

(2) Phase margin  $\geq 60^\circ \Rightarrow C_c > 0.22 C_L$

$$\text{Now } C_L = 10 \text{ pF} \Rightarrow C_c > 2.2 \text{ pF}$$

$$\text{let's use } \underline{C_c = 3 \text{ pF}}$$

(3) Slew Rate Consideration =

$$SR = \frac{I_5}{C_c} = \frac{I_5}{3 \text{ pF}} \geq 10 \text{ V}/\mu\text{s}$$

$$\Rightarrow I_5 \geq 30 \mu\text{A}$$

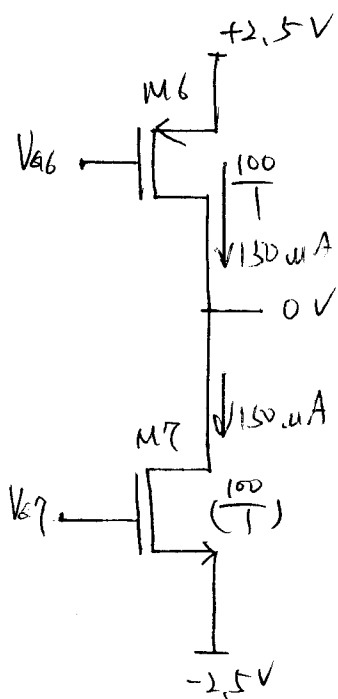
$$\text{let's use } \underline{I_5 = 30 \mu\text{A}}$$

then the output stage current  $I_{o6}$  to  $I_{o7}$ .

$$\text{are choose to be } 5 I_5 = \underline{150 \mu\text{A}}$$

then we have use 180  $\mu\text{A}$  now.

#### (4) Output stage



OVSR:

$$V_{o(max)} = 2.5 - V_{SD6(sat)}$$

$$150 = \frac{58.3}{2} \times 100 (\Delta V)^2$$

$$\Delta V = 0.227$$

$$\text{ie } \boxed{V_{o(max)} = 2.273}$$

$$V_{o(min)} = -2.5 + V_{DS7(sat)}$$

$$150 = \frac{147.86}{2} \times 100 \times (\Delta V)^2$$

$$\Delta V = 0.142$$

$$\therefore \boxed{V_{o(min)} = -2.5 + 0.142 = -2.358}$$

Therefore, OVSR = 2.273 + 2.358 = 4.631 > 4.5 (OK.)

For  $V_o = 0$ . normal bias operation.

$$M6: 150 = \frac{58.3}{2} \times 100 \times [V_{GS6} - 0.866]^2 (1 + 0.105 \times 2.5)$$

$$3 = 58.3 \times [V_{GS6} - 0.866]^2 \times 1.2625 \Rightarrow \underline{V_{GS6} = 1.066}$$

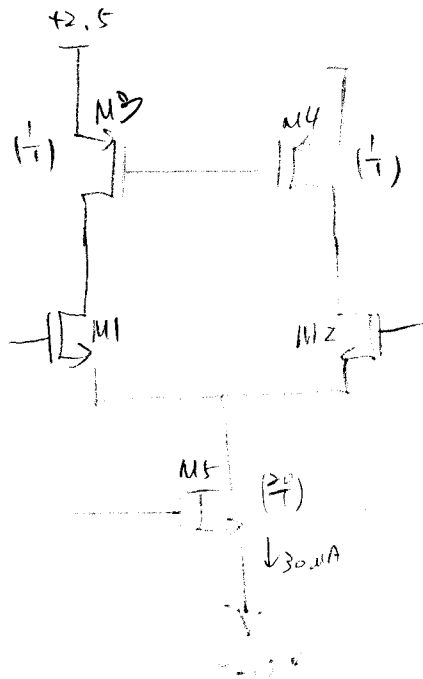
$$\text{ie } \underline{V_{G6} = 2.5 - 1.066 = 1.434 \text{ V}}$$

$$M7: 150 = \frac{147.86}{2} \times 100 \times [V_{GS7} - 0.662]^2 (1 + 0.026 \times 2.5)$$

$$3 = 147.86 [V_{GS7} - 0.662]^2 \times 1.065 \Rightarrow V_{GS7} = 0.8$$

$$\text{ie } \underline{V_{G7} = -2.5 + 0.8 = -1.7 \text{ V}}$$

# ICMR



$$V_{IC(min)} = -2.5 + V_{DS5(sat)} + V_{GS1}$$

$$30 = \frac{14786}{2} \times 20 \times V_{GS1}^2 \Rightarrow V_{GS1} = 0.142$$

$$15 = \frac{14786}{2} \times 100 \times [V_{GS1} - 0.662]^2$$

$$V_{GS1} = 0.707$$

$$\therefore V_{IC(min)} = -2.5 + 0.142 + 0.707 = -1.651$$

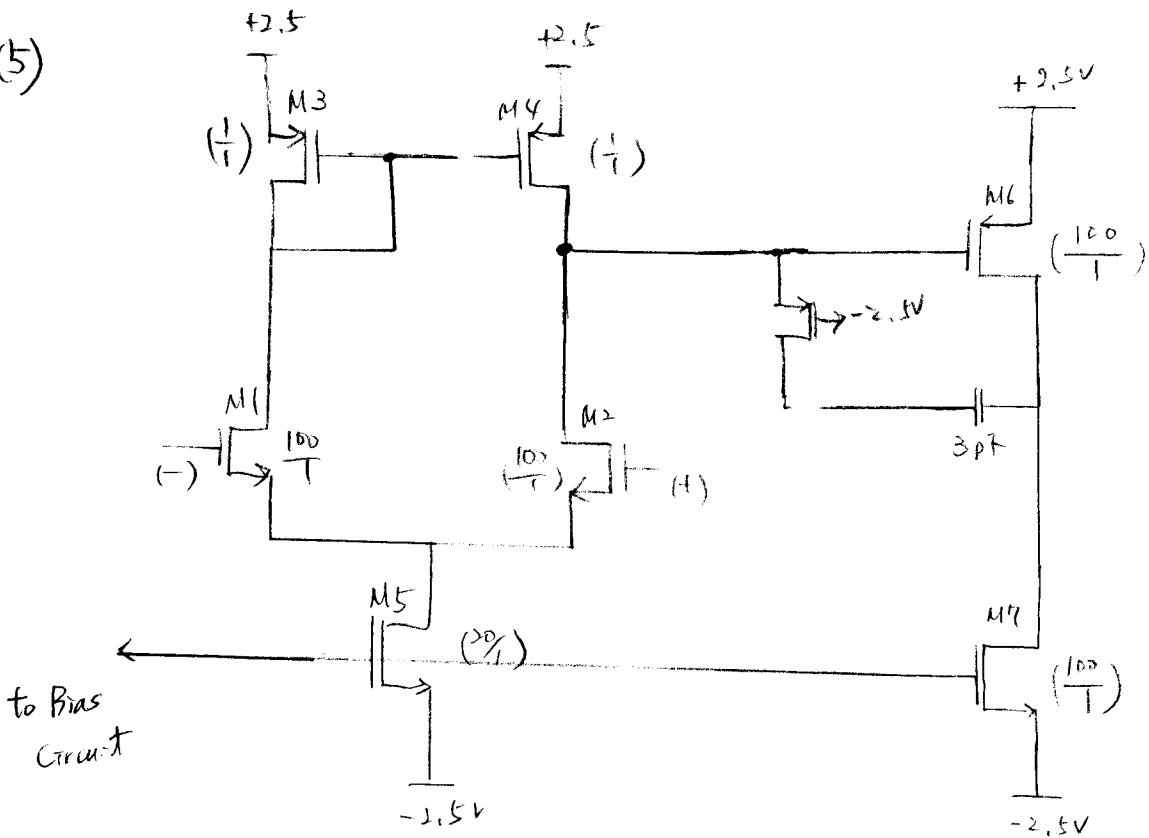
$$V_{IC(max)} = 2.5 - V_{SD4(sat)} + V_{TN}$$

$$15 = \frac{583}{2} \times 1 \times V_{TN}^2 \Rightarrow V_{TN} = 0.717$$

$$V_{IC(max)} = 2.5 - 0.717 + 0.662 = 2.445$$

$$\therefore ICMR = 2.445 + 1.651 = \underline{4.096} > 3 \text{ (ok)} \checkmark$$

(5)



(6) GB checking:

$$GB = \frac{g_{m1}}{C_c}$$

$$g_{m1} = \sqrt{2 \cdot (142.8) \cdot (100) \cdot (15)} = \underline{\underline{0.666 \text{ mS}}}$$

$$GB = \frac{0.666 \text{ mS}}{3 \text{ pF}} = 2.22 \times 10^8 \text{ rps} = \underline{\underline{35.3 \text{ MHz} > 25 \text{ MHz}}}$$

(7)  $A_{vd(\omega)}$  checking:

$$g_{mI} = g_{m2} = 0.666 \text{ mS}$$

$$r_{ds2} = \frac{1}{0.026 \times 15 \mu\text{A}} = 2.56 \text{ M}\Omega$$

$$R_I = r_{ds4} \parallel r_{ds2} = \underline{\underline{508.8 \text{ k}\Omega}}$$

$$r_{ds4} = \frac{1}{0.105 \times 15 \mu\text{A}} = 0.635 \text{ M}\Omega$$

$$g_{mII} = g_{m6} = \sqrt{2 \times 581.3 \times 100 \times 150} = \underline{\underline{1.32 \text{ mS}}}$$

$$r_{ds6} = \frac{1}{0.105 \times 150 \mu\text{A}} = 63.4 \text{ k}\Omega$$

$$R_{II} = r_{ds6} \parallel r_{ds7} = \underline{\underline{50.8 \text{ k}\Omega}}$$

$$r_{ds7} = \frac{1}{0.026 \times 150 \mu\text{A}} = 256 \text{ k}\Omega$$

$$\begin{aligned} \therefore A_{vd(\omega)} &= g_{mI} R_I g_{mII} R_{II} = 0.666 \times 508.8 \times 1.32 \times 50.8 \\ &= 2.59722 \times 10^4 = \underline{\underline{2.27 \times 10^4 > 10^4}} \end{aligned}$$



(10) check phase margin :

$$\phi = 180^\circ - \tan^{-1} \left[ \frac{GB}{|P_1|} \right] - \tan^{-1} \left[ \frac{GB}{|P_3|} \right]$$

$$= 180^\circ - \tan^{-1} \left[ \frac{2.22 \times 10^8}{6686.7} \right] - \tan^{-1} \left[ \frac{GB}{|P_3|} \right]$$

$$= 180^\circ - 89.9^\circ - \tan^{-1} \left[ \frac{GB}{|P_3|} \right]$$

$$\left[ \begin{array}{l} A_{D4} = 100 \times 10 \mu\text{m}^2, A_{D2} = 100 \times 10 \mu\text{m}^2 \text{ (ignore sidewall)} \\ C_z = C_{db4} + C_{gd4} + C_{bd2} + C_{gs2} + C_{gs4} \approx 0.482 \text{ pF} \\ f_{P3} = \frac{1}{2\pi R_z C_z} = \frac{1}{2\pi \times 3.28 \text{ k} \times 0.482 \text{ pF}} \approx 100.6 \text{ MHz} \end{array} \right]$$

$$\therefore \phi = 180^\circ - 89.9^\circ - \tan^{-1} \left[ \frac{35.3 \text{ MHz}}{100.6 \text{ MHz}} \right]$$

$$= \underline{\underline{70.76^\circ}} \#$$

(a) pole & zero.

$$\text{pole \#1 (dominant pole)} = P_1 = -\frac{g_{m1}}{A_V C_C} = -\frac{0.666 \times 10^{-3}}{3.32 \times 10^4 \times 3 \times 10^{-12}} = -\frac{0.666}{3.32 \times 3} \times 10^5 \text{ rps}$$

$$P_1 \approx 6686.7 \text{ rps} = \underline{\underline{1.06 \text{ kHz}}}$$

$$\text{pole \#2} = P_2 = -\frac{g_{m6}}{C_L} = -\frac{1.32 \times 10^{-3}}{10^{-11}} = -1.32 \times 10^8 \text{ rps}$$

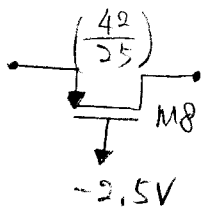
Note  $GB = 2.2 \times 10^8 \text{ rps}$  ie  $|P_2| < GB$  Need zero-nulling to earn phase margin

(1) Zero-nulling

$$\text{zero-pole cancellation} \Rightarrow \text{zero @ } \frac{-1}{R_Z C_C - C_C / g_{m6}}$$

$$\frac{-1}{R_Z C_C - C_C / g_{m6}} = -\frac{g_{m6}}{C_L} \Rightarrow g_{m6} R_Z C_C - C_C = C_L$$

$$R_Z = \frac{C_L + C_C}{g_{m6} C_C} = \frac{13 \times 10^{-12}}{1.32 \times 10^{-3} \times 3 \times 10^{-12}} = \underline{\underline{3.28 \text{ k}\Omega}}$$



$$R_Z = \frac{1}{K_P' S_8 (V_{GS} - |V_{TP}|)}$$

$$3.28 \times 10^3 = \frac{1}{58.3 \times 10^6 S_8 (3.55 - 1.864)}$$

$$S_8 = \frac{10^3}{58.3 \times 3.28 \times 2.16} = 2 \Rightarrow \frac{W}{L} = 2$$

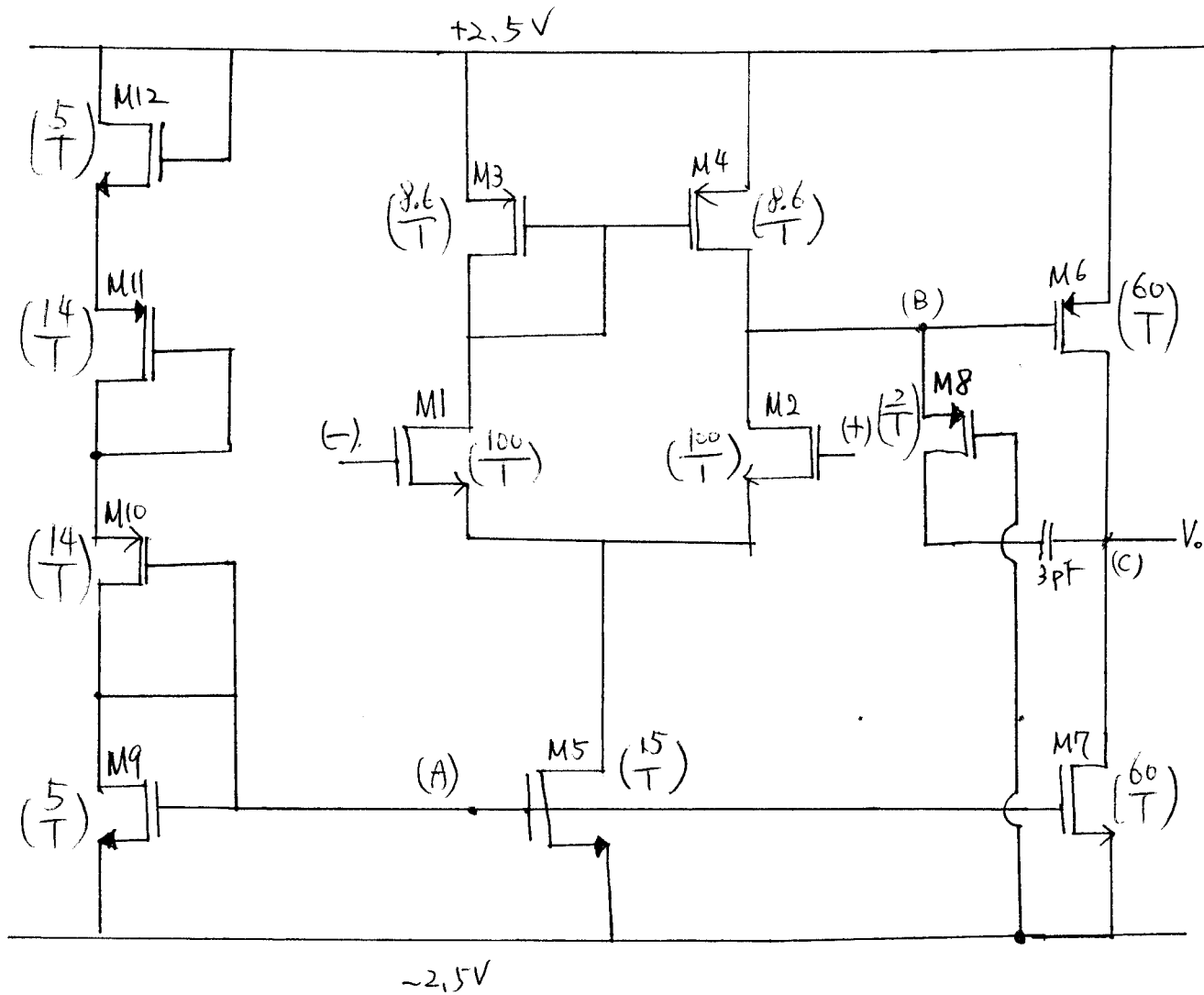
$$V_S (\text{max}) = +1.9$$

$$V_S (\text{nominal @ } +1.05V)$$

$$V_S (\text{min}) = -1.63$$

$V_{GS}$
4.4
3.55
0.87

# Final Circuit Schematic

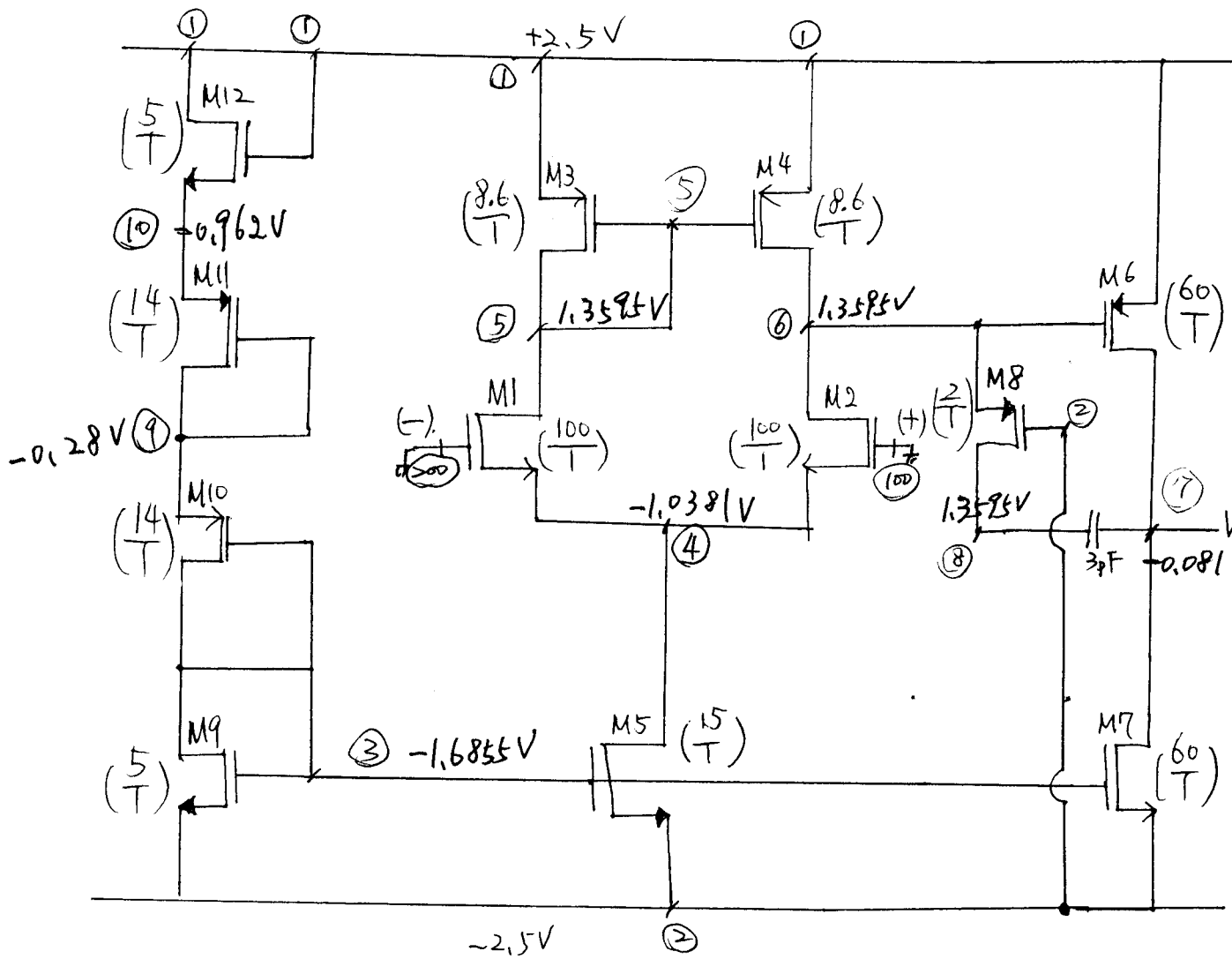


All bulks for NMOS  $\rightarrow -2.5V$

All bulks for PMOS  $\rightarrow +2.5V$

M3, M4, M6, M7, M8 are sized so that the input offset voltage is not needed. It doesn't affect the circuit performance as long as @  $V_{in} = 0, V_{out} = 0$ .  
 (A), (B), (C) "3" points are biased at the correct operating points.

Final Circuit Schematic (D.C. Bias condition.  $V_+ = V_- = \text{GND}$ )



All bulks for NMOS  $\rightarrow -2.5V$

All bulks for PMOS  $\rightarrow +2.5V$